



The Quest for Correctness - Beyond *a posteriori* Verification


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in collaboration with

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Correctness by checking vs. Correctness by construction

Building systems which are correct with respect to given requirements is the main challenge for all engineering disciplines

Correctness can be achieved:

- Either by checking that a system or a model of a system meets given requirements
- Or by construction by using results such as algorithms, protocols, architectures e.g. token ring protocol, time triggered architecture

A big difference between Computing Systems Engineering and disciplines based on Physics is the importance of a *posteriori* verification for achieving correctness



Current status

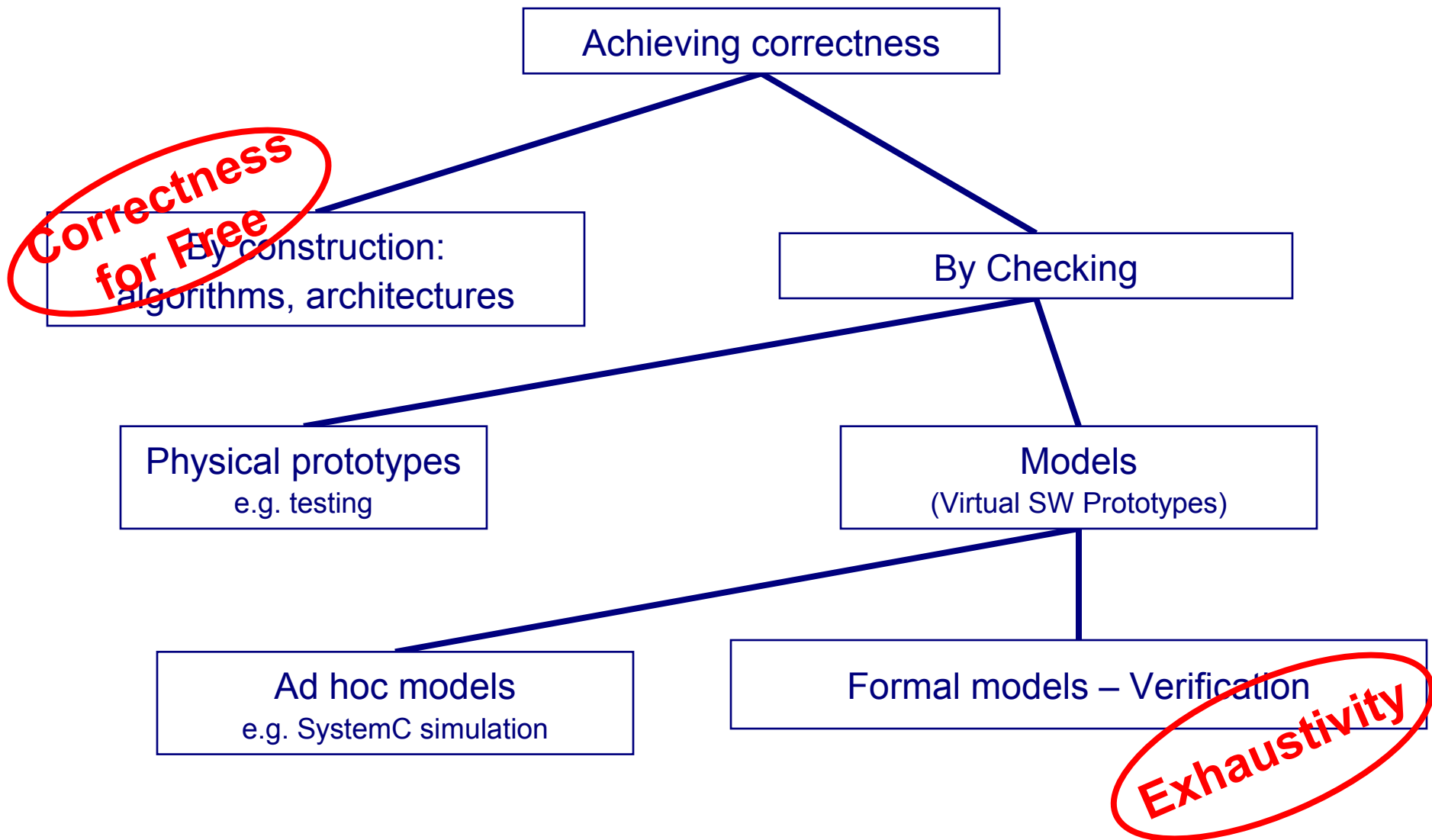
Beyond a posteriori verification

- Component-based Construction
- The BIP Component Framework
- Verification at Design Time

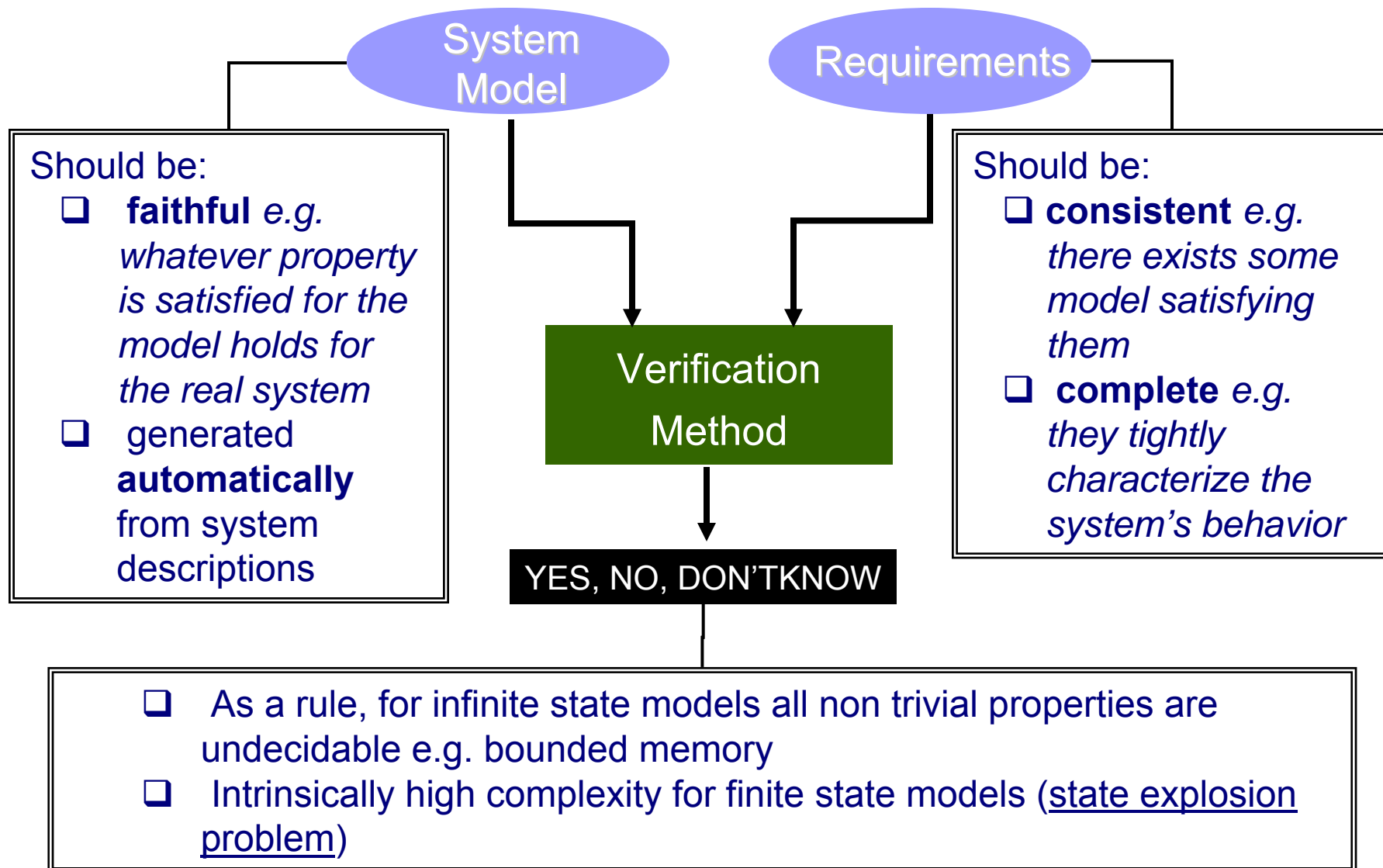
Conclusion

Achieving Correctness

Correctness: a system is correct if it meets its requirements



A posteriori Verification



Develop “divide and conquer” verification techniques

- Taking advantage of system structure and its properties e.g. for particular
 - architectures (e.g. client-server, star-like, time triggered)
 - programming models (e.g. synchronous, data-flow)
 - execution models (e.g. event triggered preemptable tasks)

- For specific classes of properties such as deadlock-freedom, mutual exclusion, timeliness

Beyond *a posteriori* Verification – Principles

- ❑ Component-based and faithful construction of models from heterogeneous components

- ❑ Tight coupling between design and verification - Achieving correctness through
 - Constructivity: compositionality/composability techniques
 - Incrementality: reusing proofs for constituents
 - Property-preserving transformations

- ❑ Minimalistic verification framework
 - Focus on state invariants and deadlock-freedom



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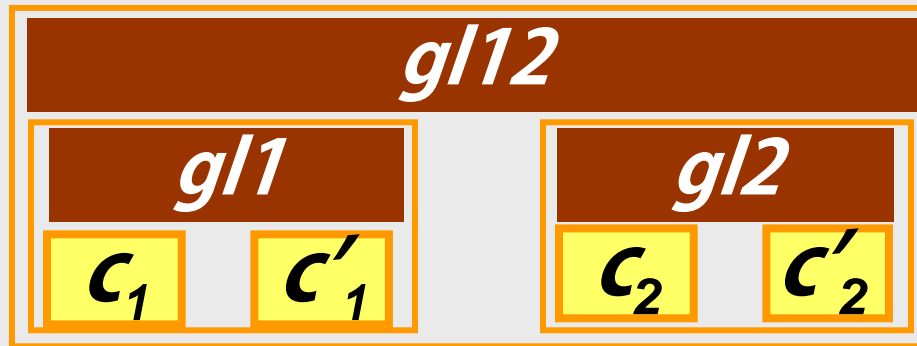
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Component-based Construction

Build a component C satisfying given requirements f , from

- \mathcal{C}_0 a set of **atomic** components described by their behavior
- $\mathcal{GL} = \{gl_1, \dots, gl_i, \dots\}$ a set of **glue operators** on components

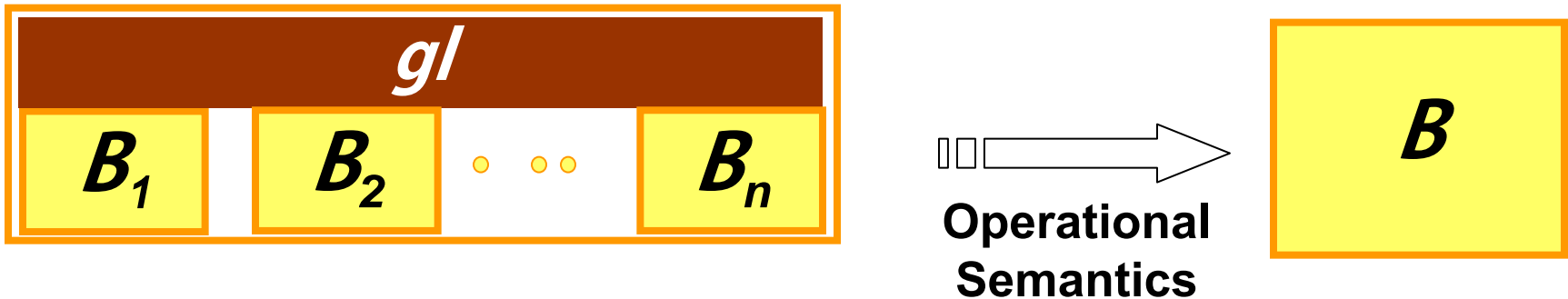


satisfies f

- ❑ Move from single low-level composition operators e.g. automata-based to families of high-level composition operators e.g. protocols, controllers
- ❑ We need a unified composition paradigm for describing and analyzing the coordination between components to formulate heterogeneous system designs in terms of tangible, well-founded and organized concepts

Glue Operators – Operational Semantics

We use operational semantics to define the meaning of a composite component – glue operators are “behavior transformers”



Glue Operators

- build interactions of composite components from the actions of the atomic components e.g. parallel composition operators
- can be specified by using a family of derivation rules (the Universal Glue)

Glue Operators – Operational Semantics

A **glue operator** is a set of derivation rules of the form

$$\frac{\{q_i - a_i \rightarrow_i q'_i\}_{i \in I} \quad \{\neg q_k - a_k \rightarrow_k\}_{k \in K}}{(q_1, \dots, q_n) - a \rightarrow (q'_1, \dots, q'_n)}$$

- $I, K \subseteq \{1, \dots, n\}$, $I \neq \emptyset$, $K \cap I = \emptyset$
- $a = \bigcup_{i \in I} a_i$ is an interaction
- $q'_i = q_i$ for $i \notin I$

Notice that, non deterministic choice and sequential composition are not glue operators

A **glue** is a set of glue operators

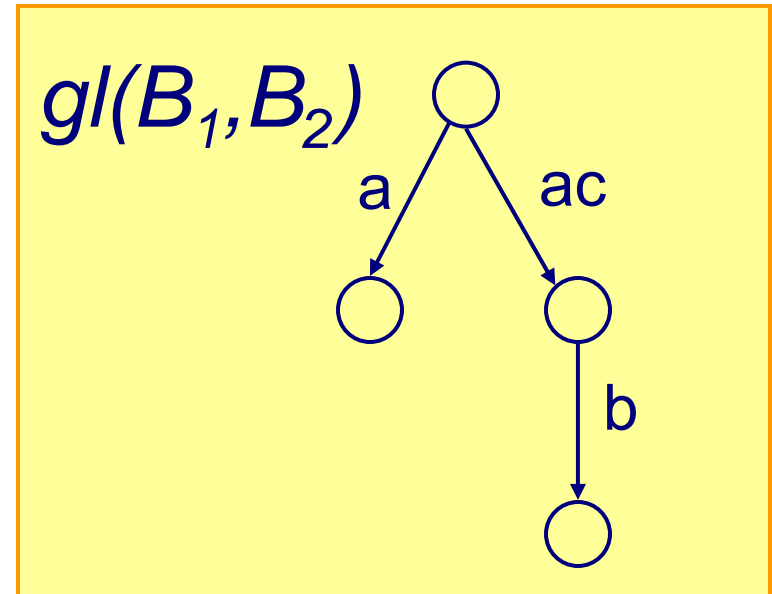
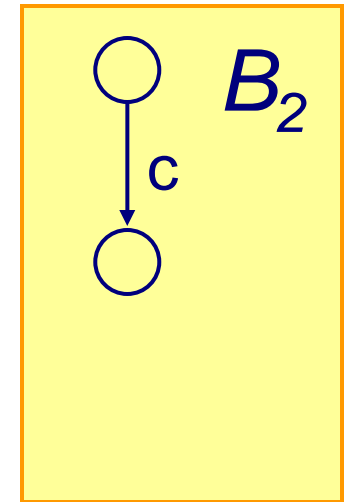
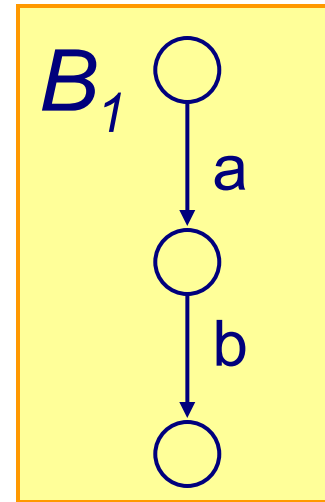
Glue Operators – Operational Semantics: Example

gl is defined by

$$\frac{q_1 - a \rightarrow q'_1}{q_1 q_2 - a \rightarrow q'_1 q_2}$$

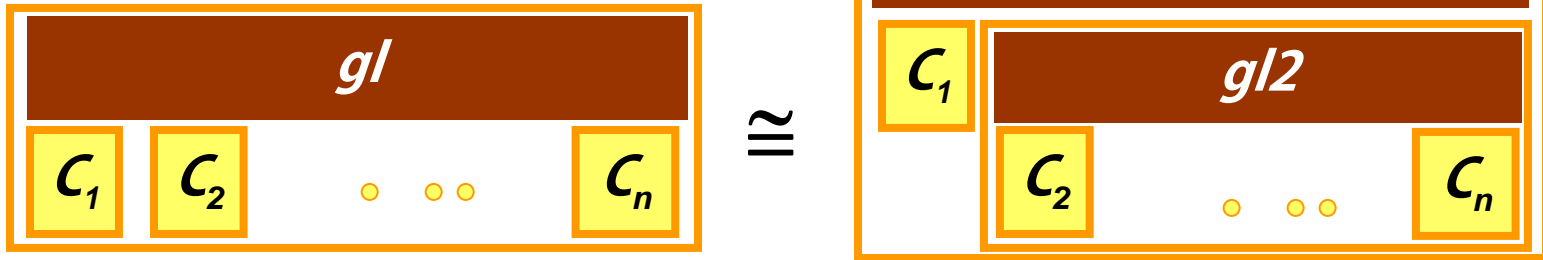
$$\frac{q_1 - a \rightarrow q'_1 \quad q_2 - c \rightarrow q'_2}{q_1 q_2 - ac \rightarrow q'_1 q'_2}$$

$$\frac{q_1 - b \rightarrow q'_1 \quad \neg q_2 - c \rightarrow}{q_1 q_2 - b \rightarrow q'_1 q_2}$$

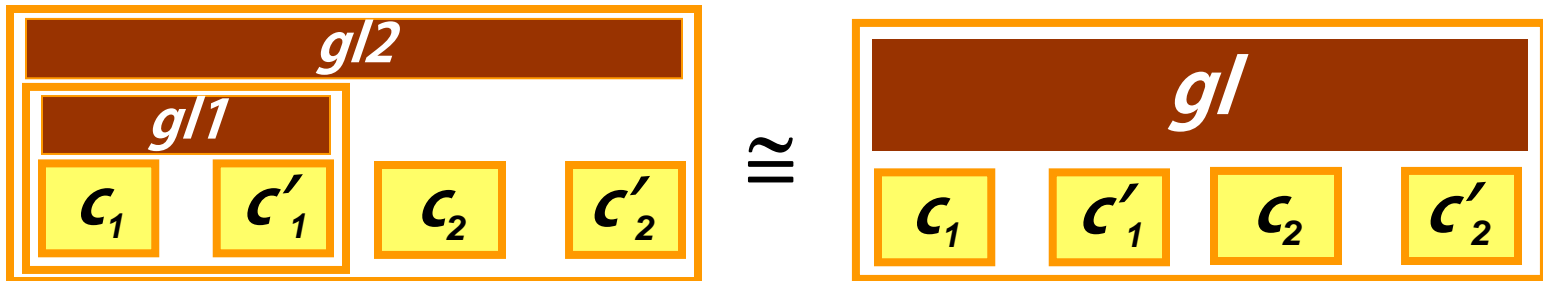


Glue Operators – Incremental Construction

1. Decomposition



2. Flattening



Glue Operators – Compositionality

Build correct systems from correct components: rules for proving global properties from properties of individual components



C_i sat P_i implies $\forall gl \exists \tilde{gl}$

gl
 $C_1 \dots C_n$ sat $\tilde{gl}(P_1, \dots, P_n)$

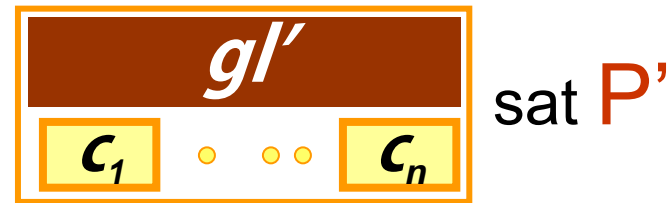
We need compositionality results for the preservation of progress properties such as deadlock-freedom and liveness as well as extra-functional properties

Glue Operators – Composability

Essential properties of components are preserved when they are composed



sat P and



sat P'

implies



sat $P \wedge P'$

*Property stability phenomena are poorly understood.
We need composability results e.g. non interaction of features in middleware,
composability of scheduling algorithms, composability of web services*

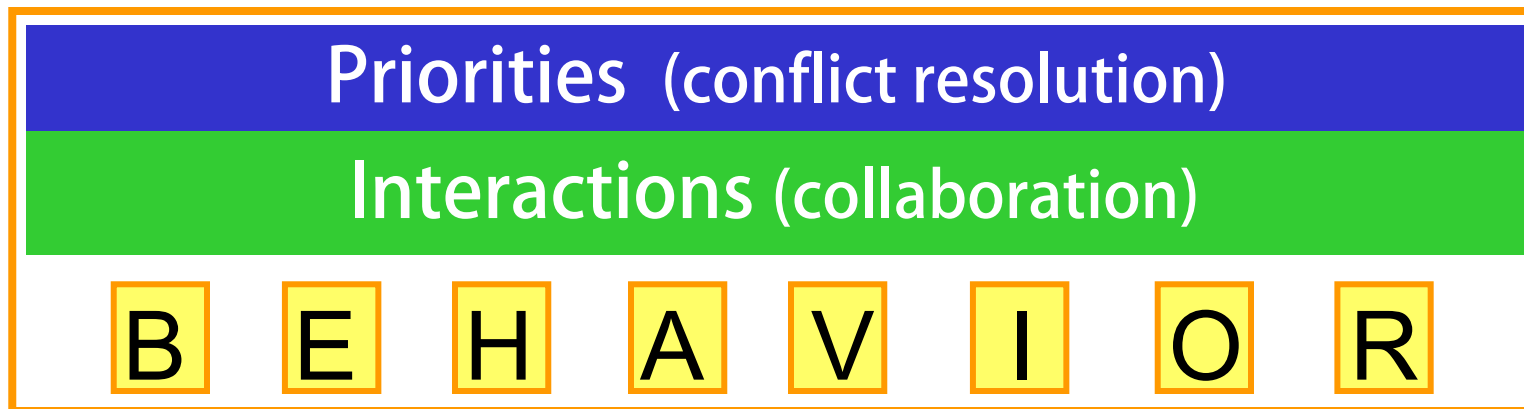
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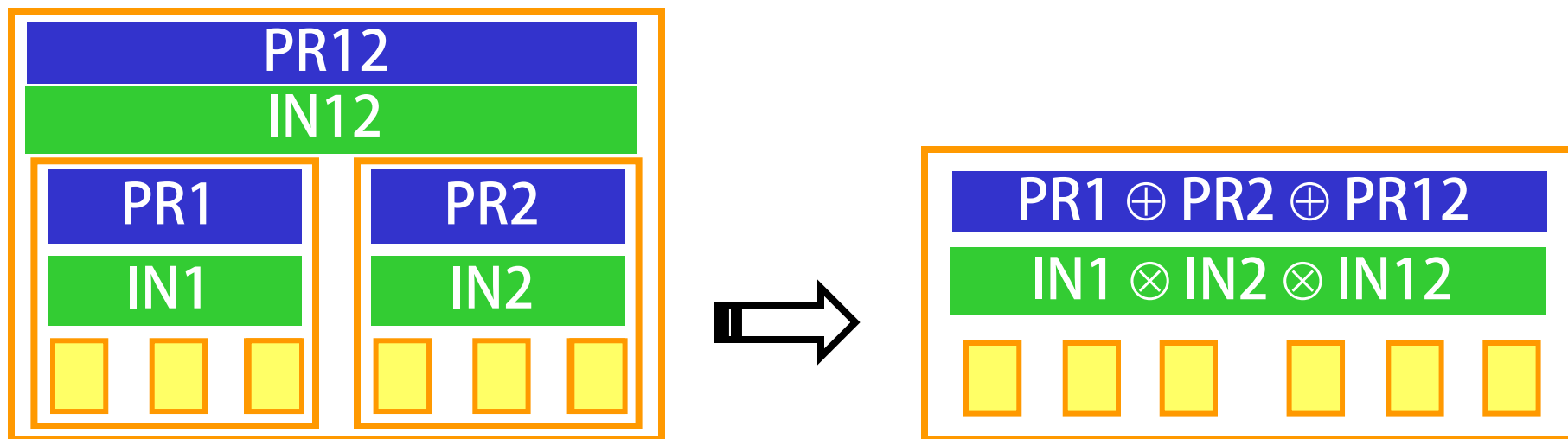
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BIP – Basic Concepts

Layered component model

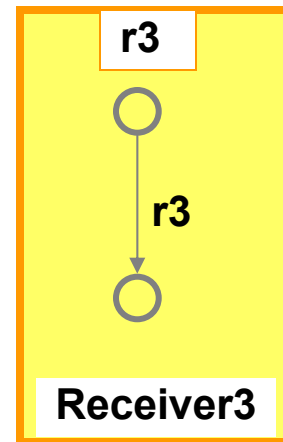
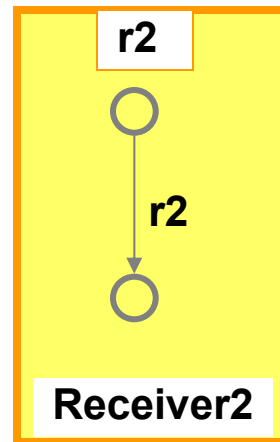
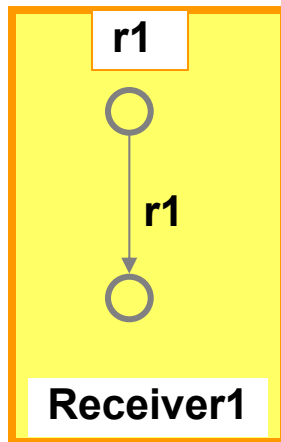
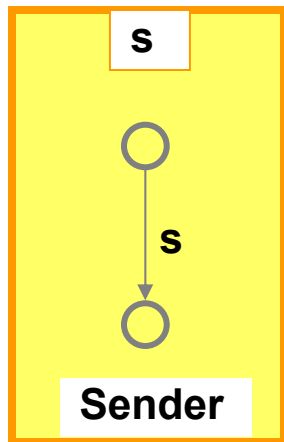


Composition operation parameterized by glue IN12, PR12



Priorities: \emptyset

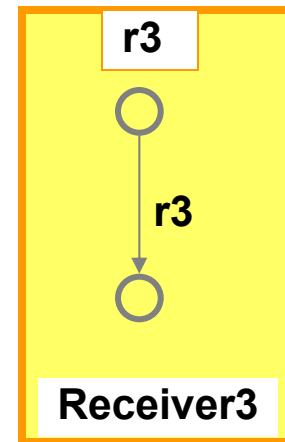
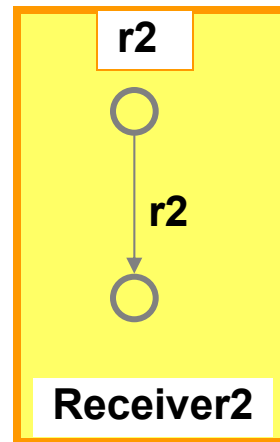
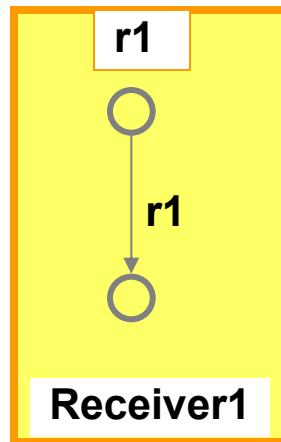
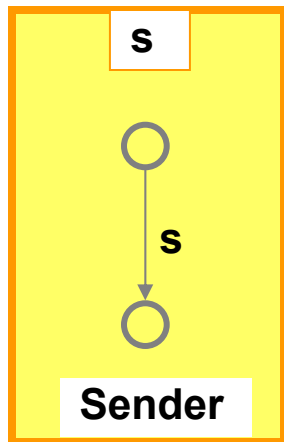
Interactions: sr1r2r3



Rendezvous

Priorities: $x \prec xy$ for $x, xy \in \text{Interactions}$

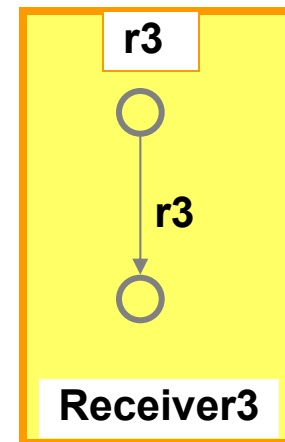
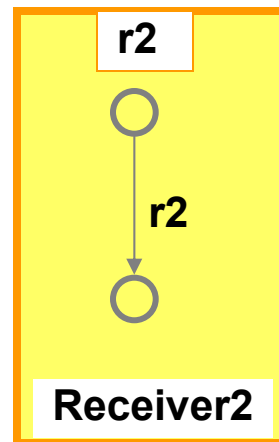
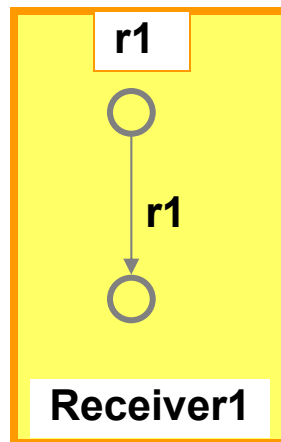
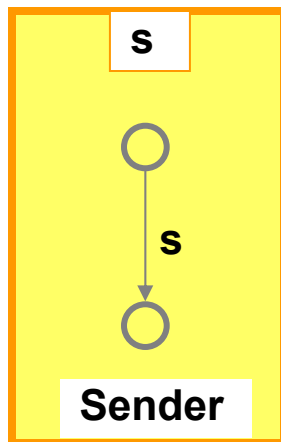
Interactions: $s + sr1 + sr2 + sr3 + sr1r2 + sr2r3 + sr1r3 + sr1r2r3$



Broadcast

Priorities: $x \prec xy$ for $x, xy \in \text{Interactions}$

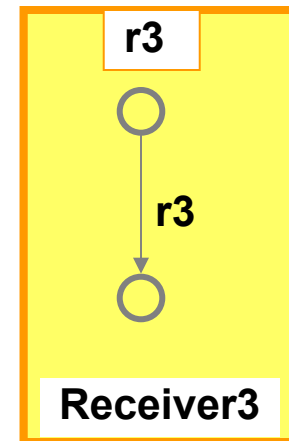
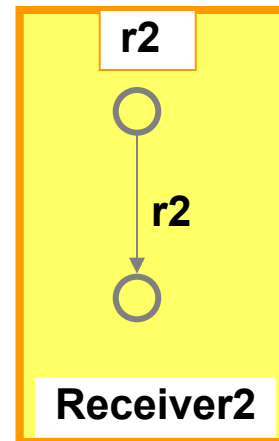
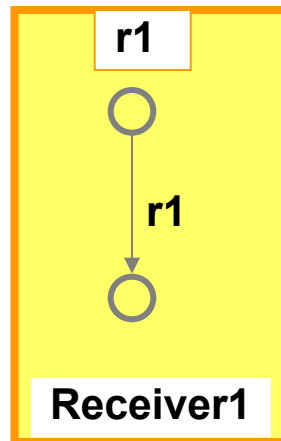
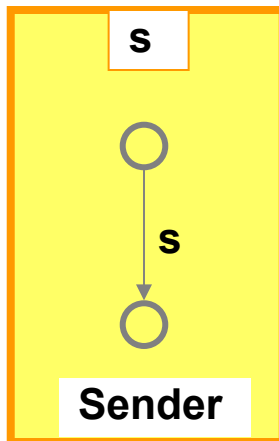
Interactions: $s + sr_1r_2r_3$



Atomic Broadcast

Priorities: $x \prec xy$ for $x, xy \in \text{Interactions}$

Interactions: $s + sr1 + sr1r2 + sr1r2r3$



Causal Chain

- a set of atomic components $\{B_i\}_{i=1..n}$
where $B_i = (Q_i, 2^{P_i}, \rightarrow_i)$
 - a set of interactions γ
 - priorities π , partial order on interactions
- } $\pi \gamma (B_1, \dots, B_n)$

Interactions

$$\frac{a \in \gamma \wedge \forall i \in [1, n] \ q_i - a \cap P_i \rightarrow_i q'_i}{(q_1, \dots, q_n) - a \rightarrow_\gamma (q'_1, \dots, q'_n) \text{ where } q'_i = q_i \text{ if } a \cap P_i = \emptyset}$$

Priorities

$$\frac{q - a \rightarrow_\gamma q' \wedge \neg (\exists q - b \rightarrow_\gamma \wedge a \pi b)}{q - a \rightarrow_\pi q'}$$

- Current status

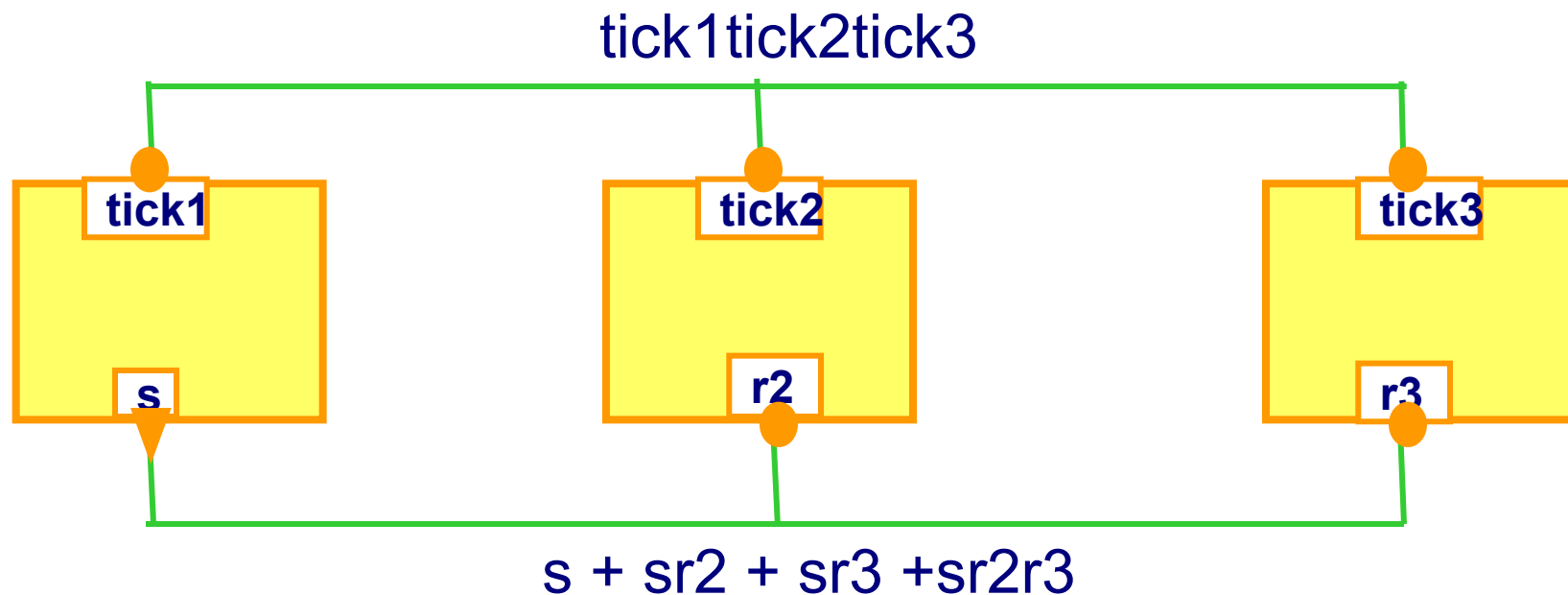
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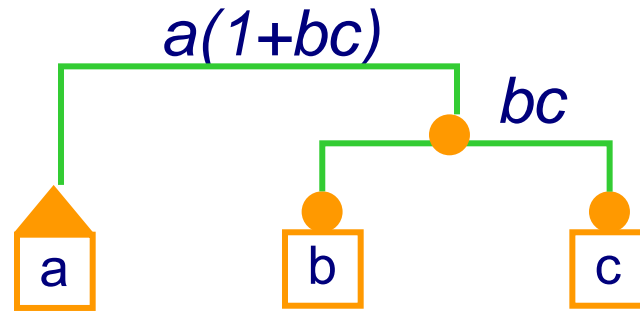
Modeling Interactions – Simple Connectors

Express interactions by combining two protocols: rendezvous and broadcast

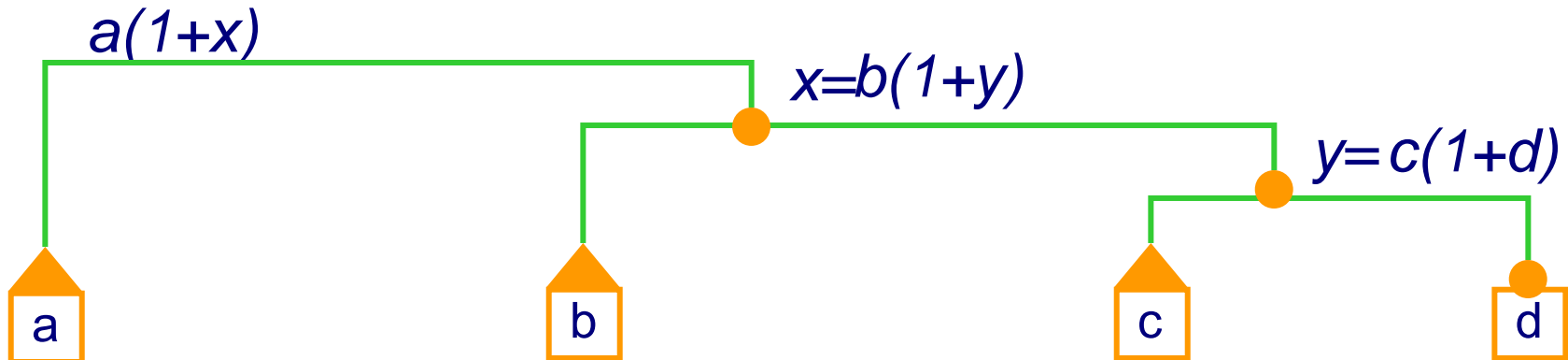
- A **connector** is a set of ports that can be involved in an interaction
- Port attributes (**trigger** ▼ , **synchron** ●) are used to model rendezvous and broadcast.
- An **interaction** of a connector is a set of ports such that: either it contains some trigger or it is maximal.



Atomic Broadcast:
 $a+abc$



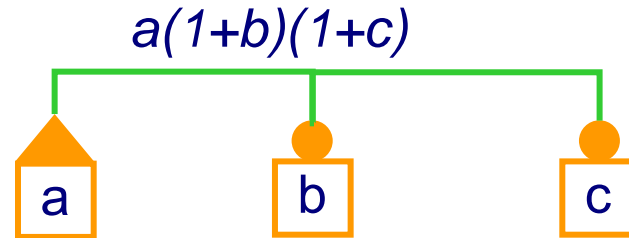
Causality chain: $a+ab+abc+abcd$



Modeling Interactions – The Algebra of Connectors

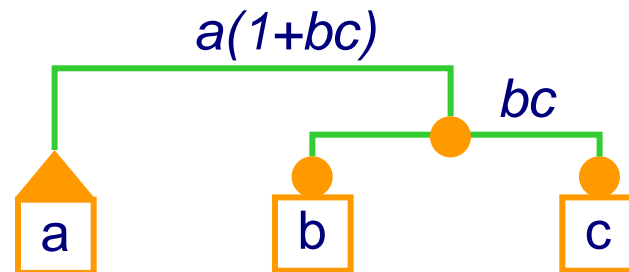
Broadcast

$a'bc$



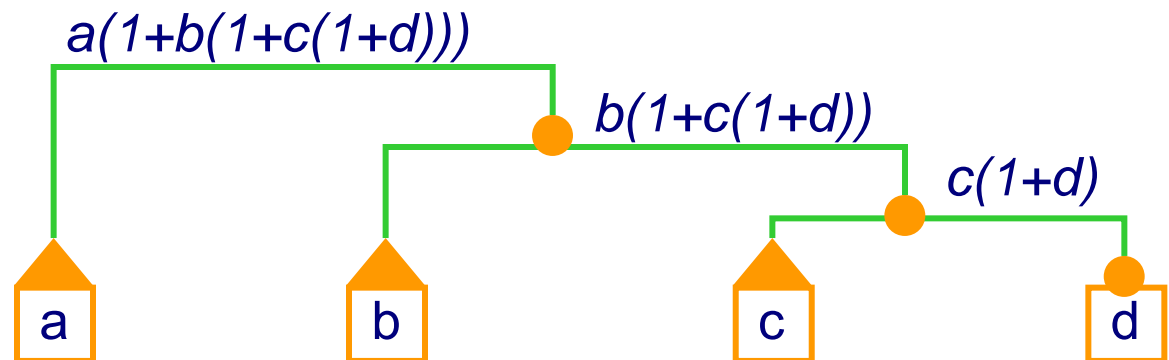
Atomic Broadcast

$a'[bc]$

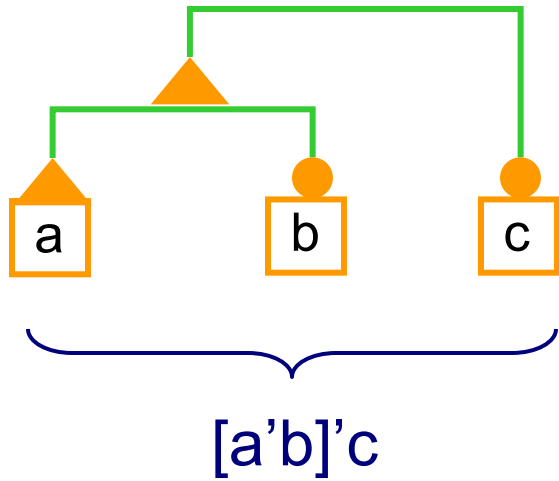


Causality chain

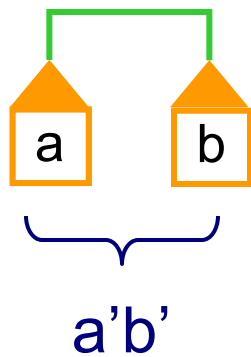
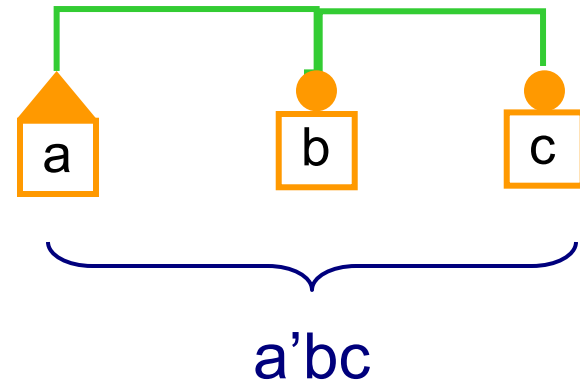
$a'[b'[c'd]]$



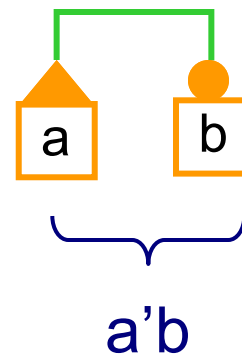
Modeling Interactions – The Algebra of Connectors



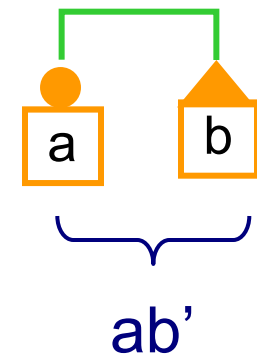
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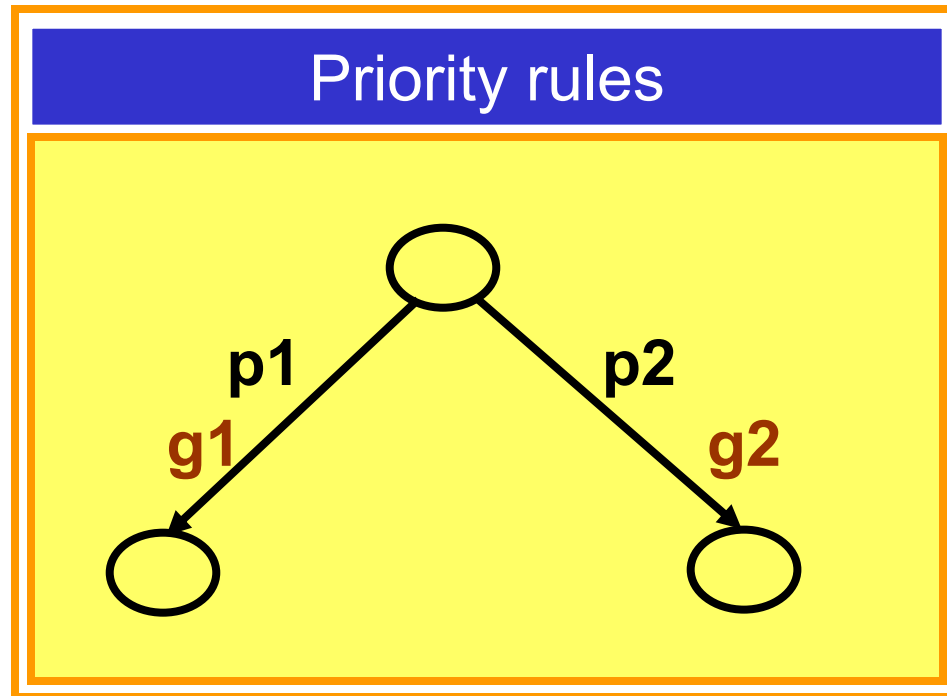
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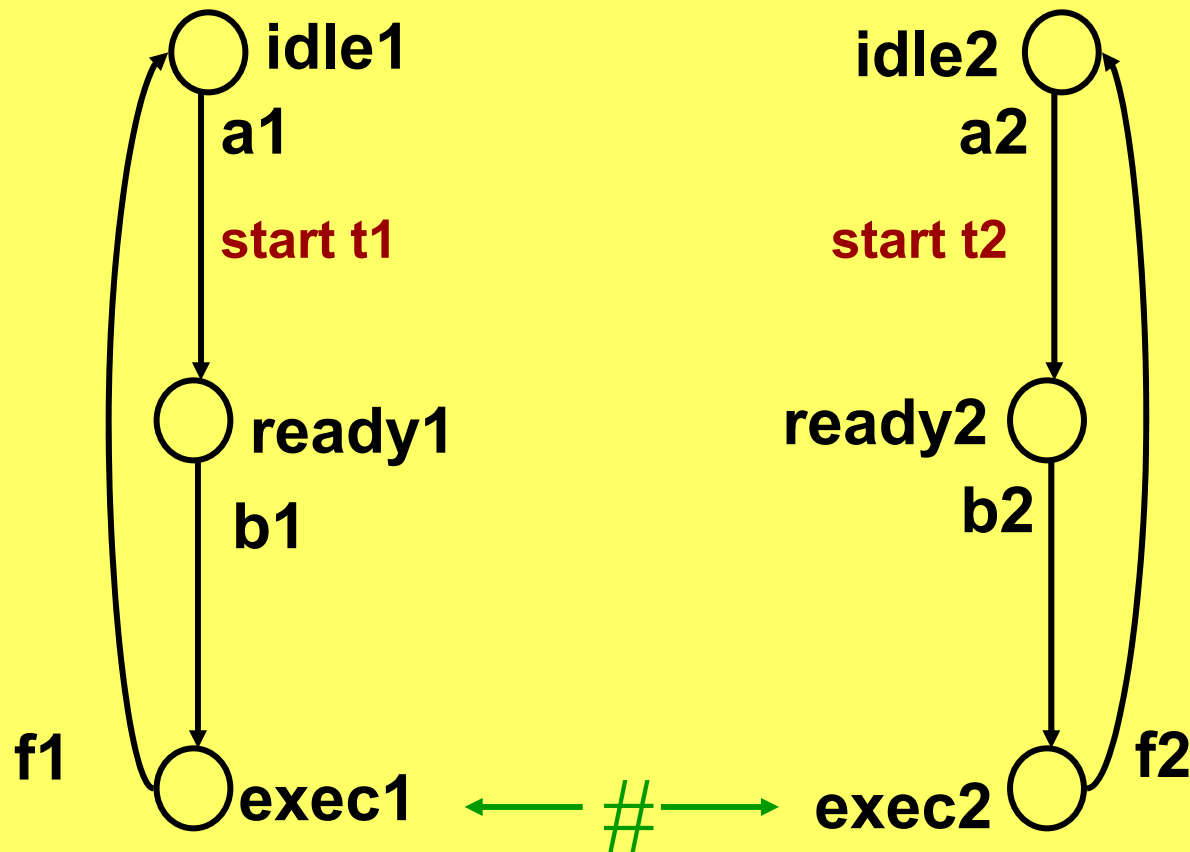
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Priority rule	Restricted guard $g1'$
$\text{true} \rightarrow p1 \prec p2$	$g1' = g1 \wedge \neg g2$
$C \rightarrow p1 \prec p2$	$g1' = g1 \wedge \neg(C \wedge g2)$

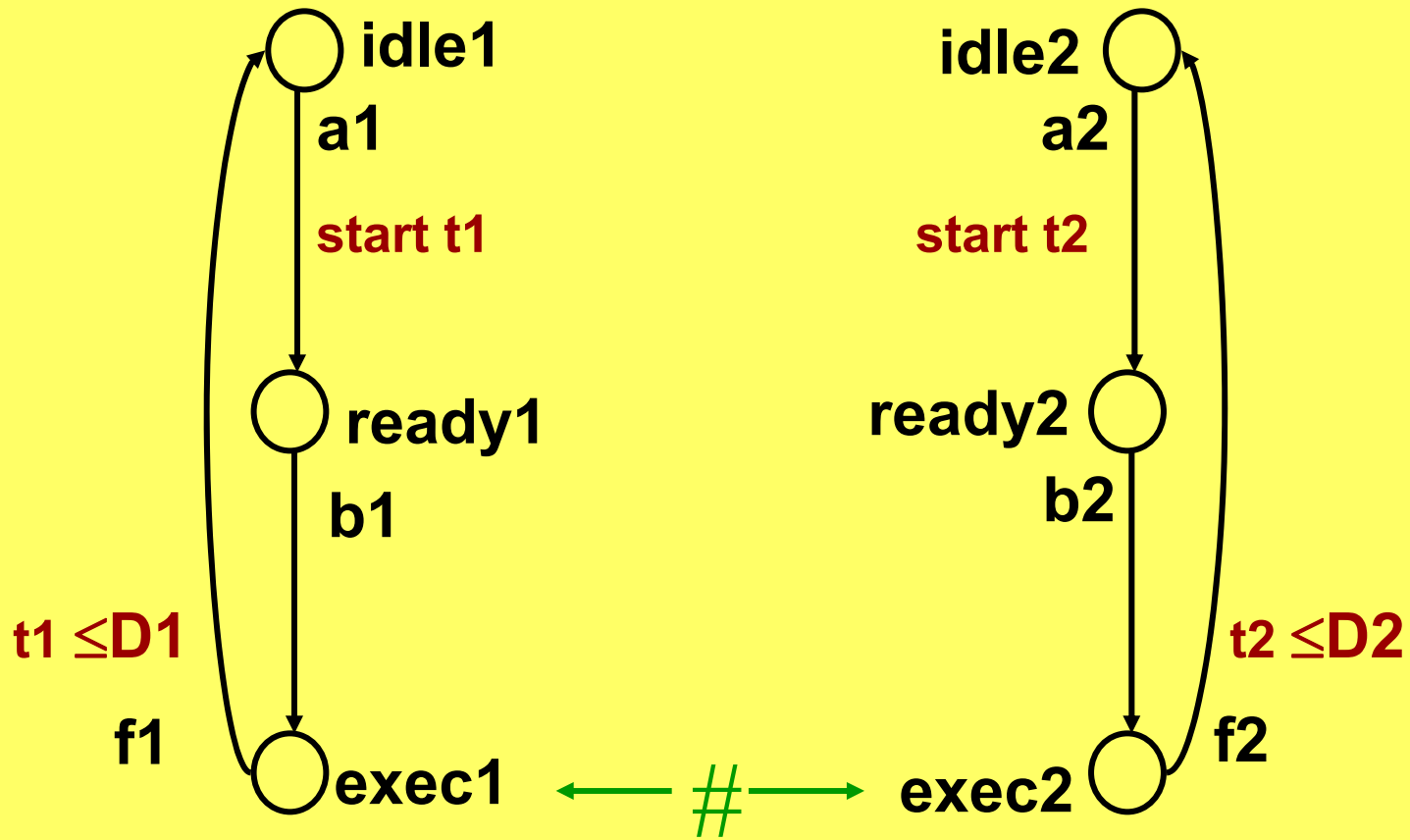
Modeling Priorities – FIFO policy

PR : $t1 \leq t2 \rightarrow b1 \langle b2$ $t2 < t1 \rightarrow b2 \langle b1$

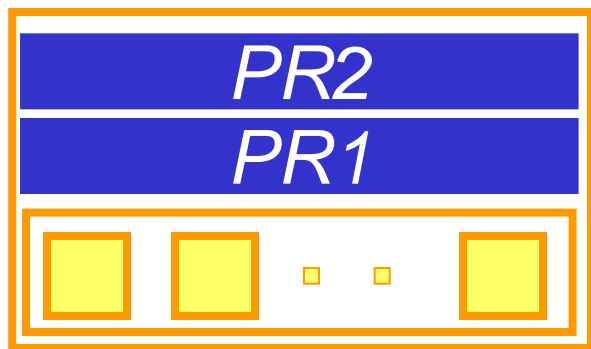


Modeling Priorities – EDF policy

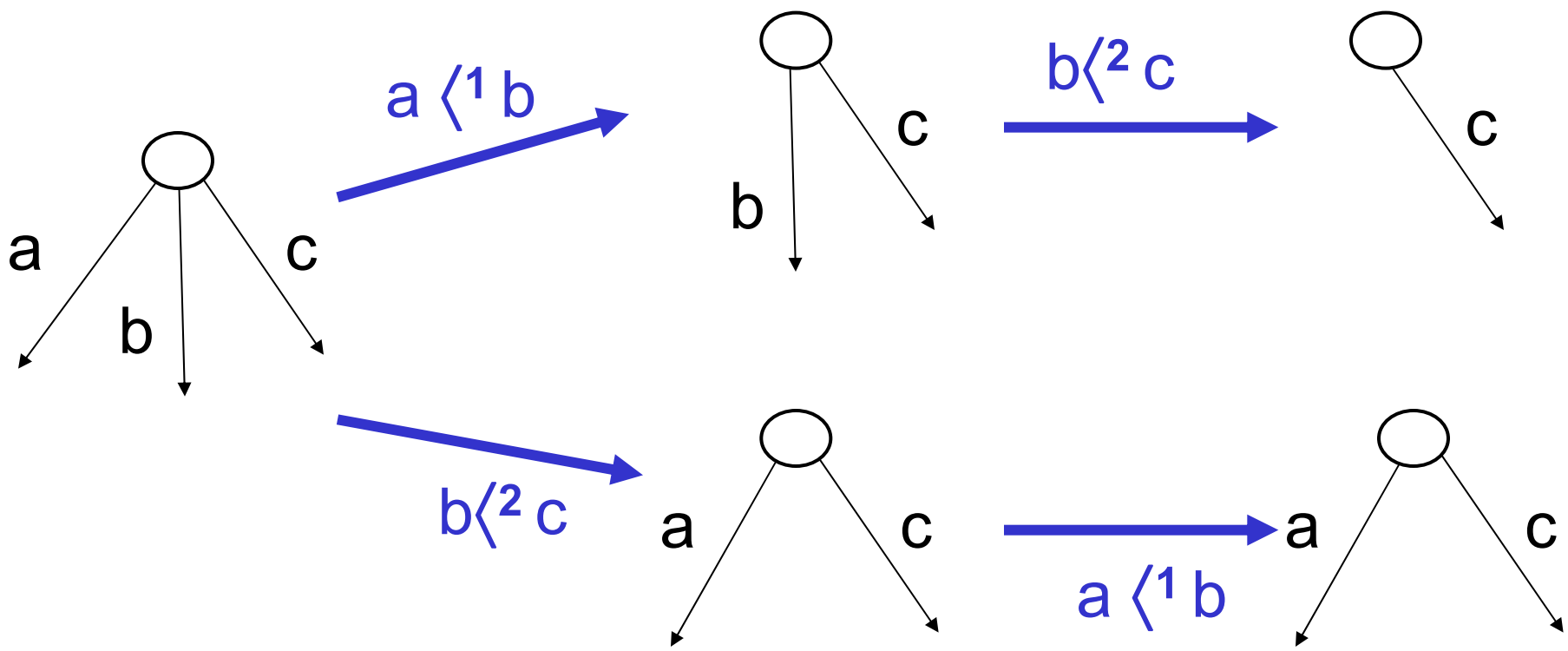
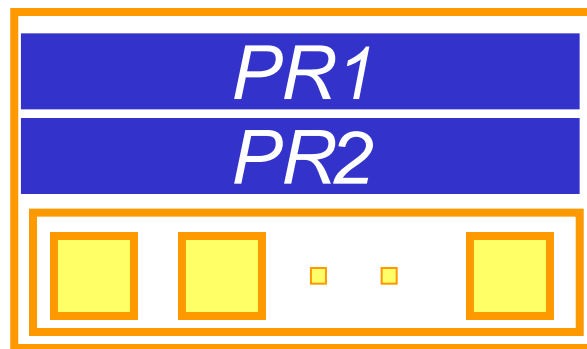
PR: $D1-t1 \leq D2-t2 \rightarrow b2 \prec b1$ $D2-t2 < D1-t1 \rightarrow b1 \prec b2$



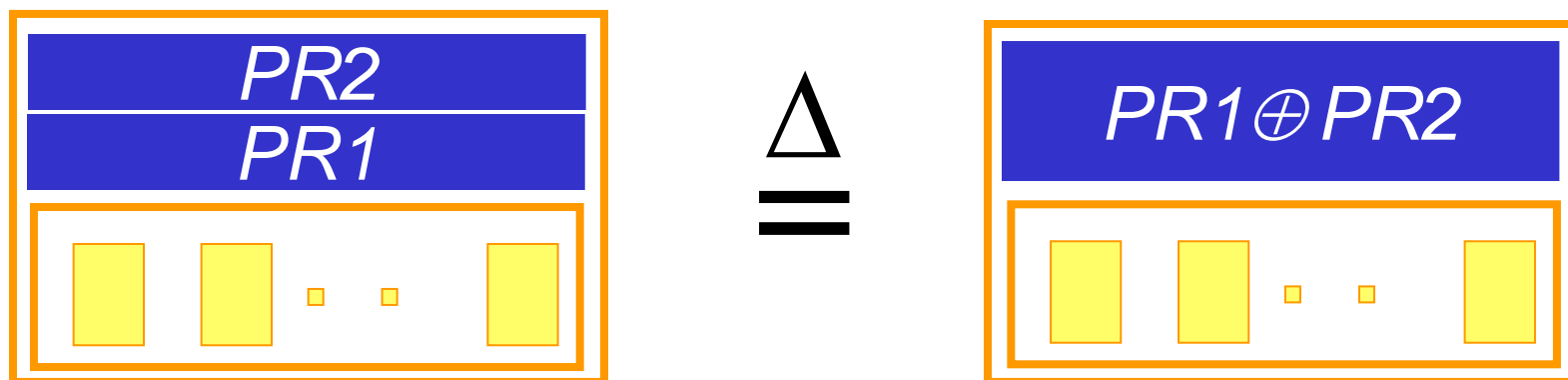
Modeling Priorities – Composability



\neq



We take:



$PR1 \oplus PR2$ is the least priority containing $PR1 \cup PR2$

Results :

- The operation \oplus is partial, associative and commutative
- $PR1(PR2(B)) \neq PR2(PR1(B))$
- $PR1 \oplus PR2(B)$ *refines* $PR1 \cup PR2(B)$ *refines* $PR1(PR2(B))$
- Priorities preserve deadlock-freedom

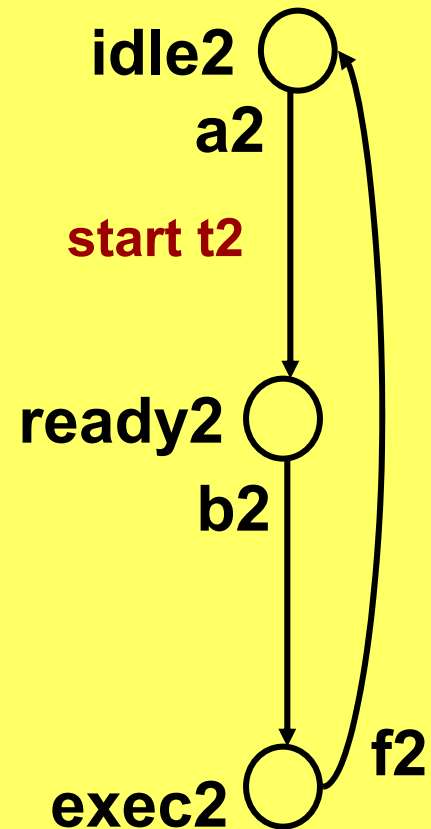
Modeling Priorities – Mutual Exclusion + FIFO policy

$t1 \leq t2 \rightarrow b1 \prec b2$

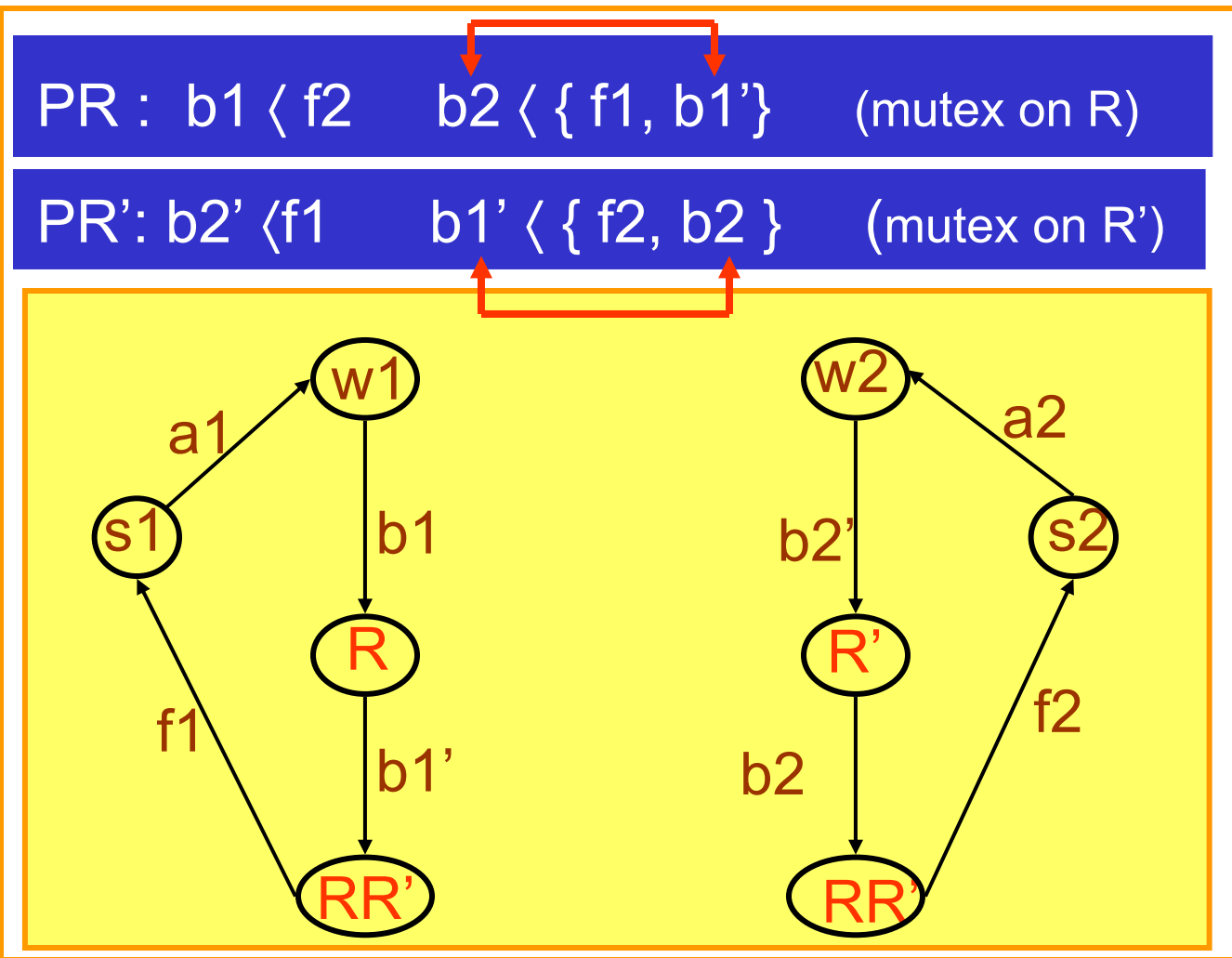
$t2 < t1 \rightarrow b2 \prec b1$

$true \rightarrow b1 \prec f2$

$true \rightarrow b2 \prec f1$



Modeling Priorities – Mutual Exclusion: Example



Risk of deadlock: $PR \oplus PR'$ is not defined

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Expressiveness for Component-based Systems

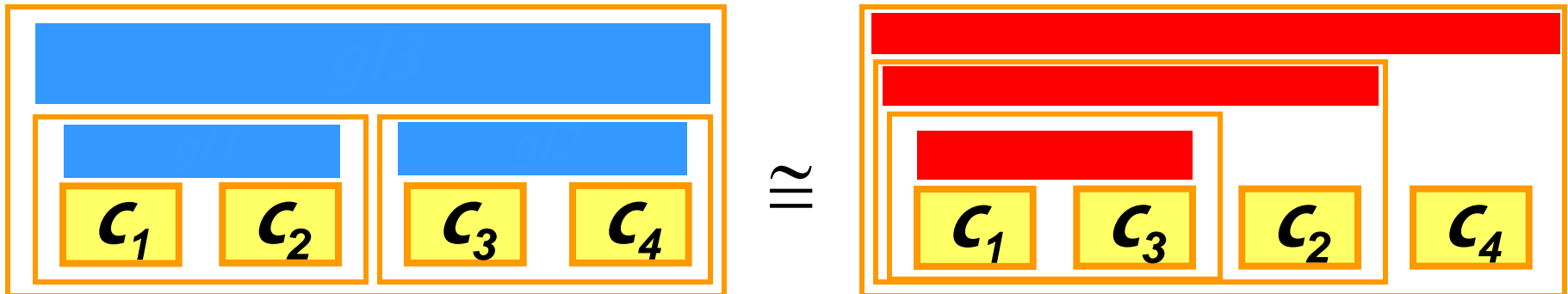
- Different from the usual notion of expressiveness!
- Based on strict separation between glue and behavior

Given two glues G_1 , G_2

G_2 is *strongly more expressive than* G_1

if for any component built by using G_1 and \mathcal{C}_0

there exists an equivalent component built by using G_2 and \mathcal{C}_0



Expressiveness for Component-based Systems

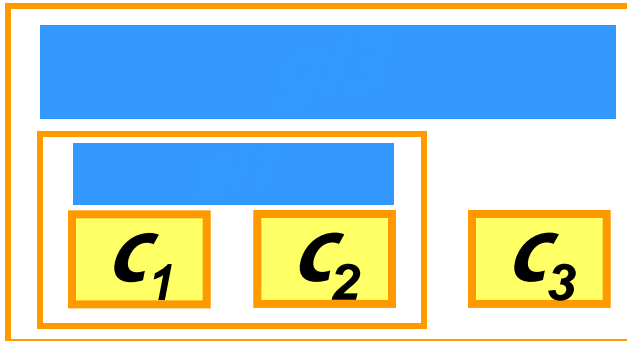
Given two glues G_1, G_2

G_2 is weakly more expressive than G_1

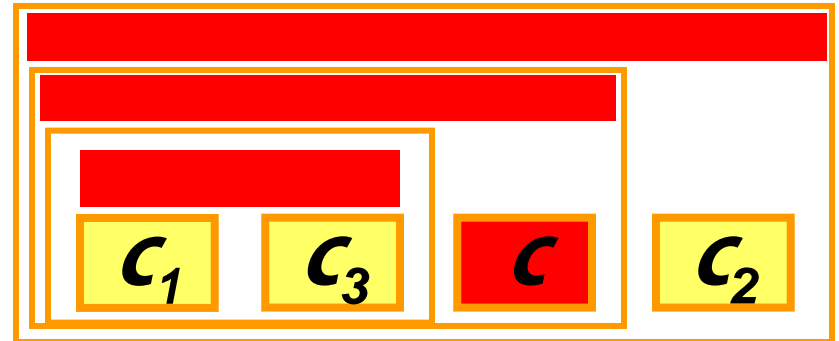
if for any component built by using G_1 and \mathcal{C}_0

there exists an equivalent component built by using G_2 and $\mathcal{C}_0 \cup \mathcal{C}$

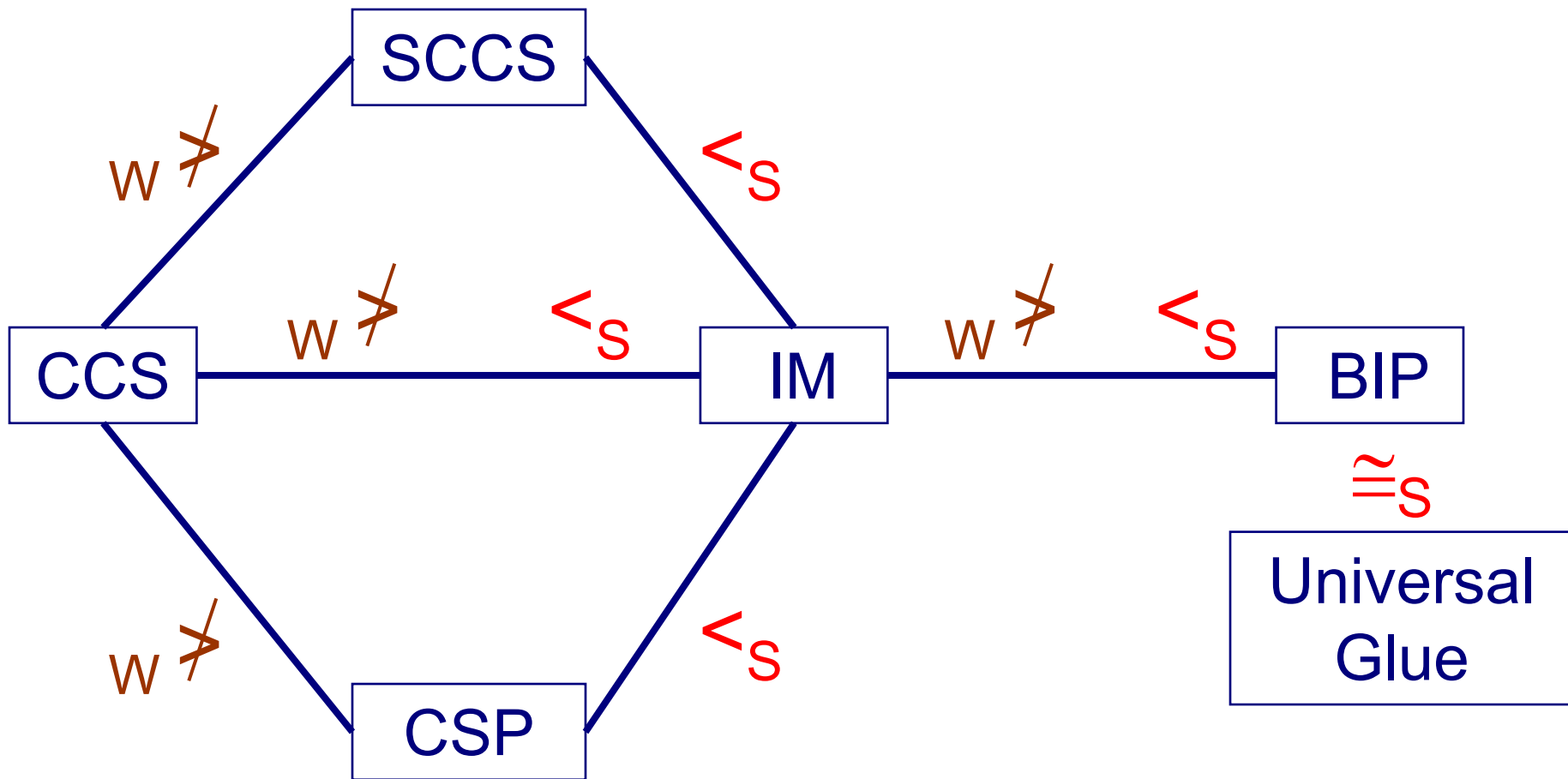
where \mathcal{C} is a finite set of coordination behaviors.



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Expressiveness for Component-based Systems





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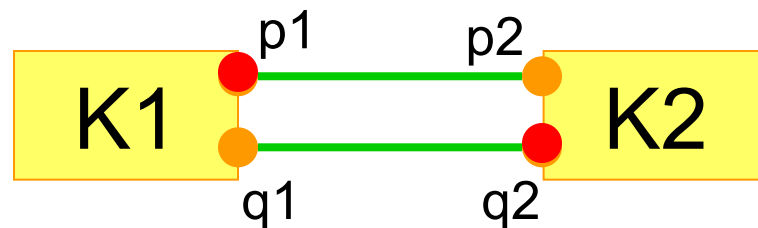
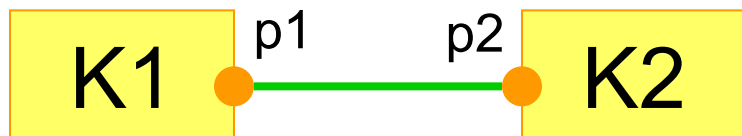
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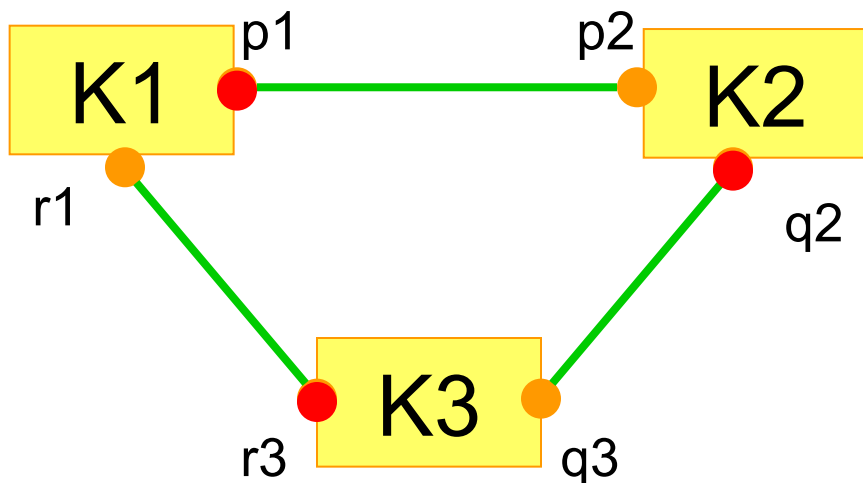
Compositional Verification

Verify global deadlock-freedom of a system by separate analysis of the components and of the architecture.



Potential deadlock

$$D = en(p1) \wedge \neg en(p2) \wedge en(q2) \wedge \neg en(q1)$$



Potential deadlock

$$D = en(p1) \wedge \neg en(p2) \wedge en(q2) \wedge \neg en(q3) \wedge en(r3) \wedge \neg en(r1)$$

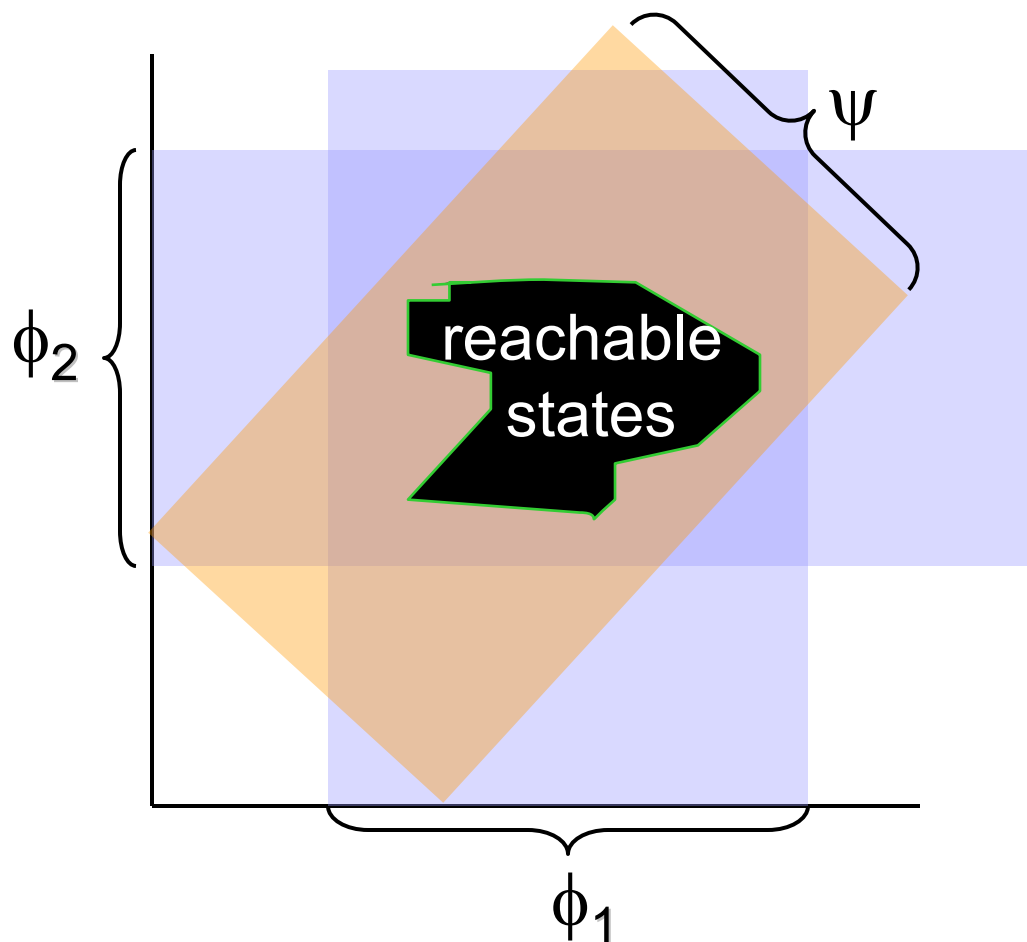
Compositional Verification: D-Finder

$$B_1 \models \Box \phi_1 \quad B_2 \models \Box \phi_2 \quad \psi \in \Pi(\gamma(B_1, B_2), \phi_1, \phi_2) \quad \phi_1 \wedge \phi_2 \wedge \psi \Rightarrow \chi$$

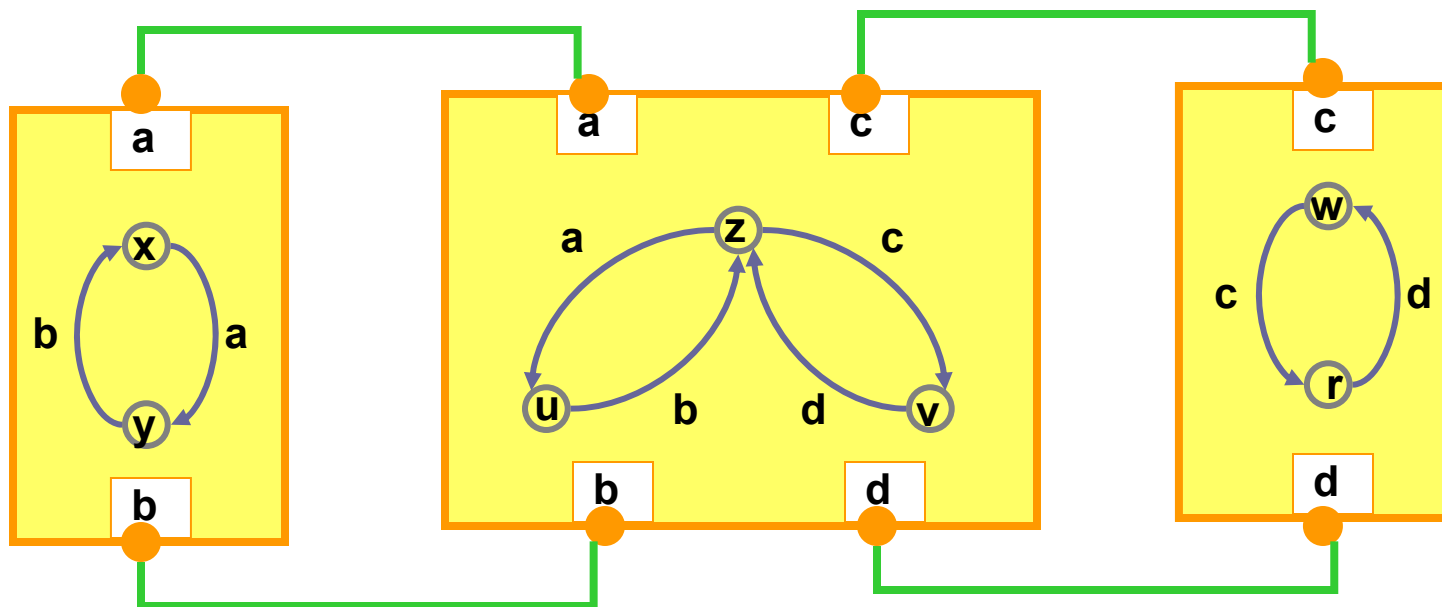
$$\gamma(B_1, B_2) \models \Box \chi$$

Method:

Eliminate potential deadlocks D by computing compositionally global invariants χ such that $\chi \wedge D = \text{false}$



Compositional Verification – D-Finder



$$\begin{array}{l} x \Rightarrow y \vee u \\ y \Rightarrow x \vee z \end{array}$$

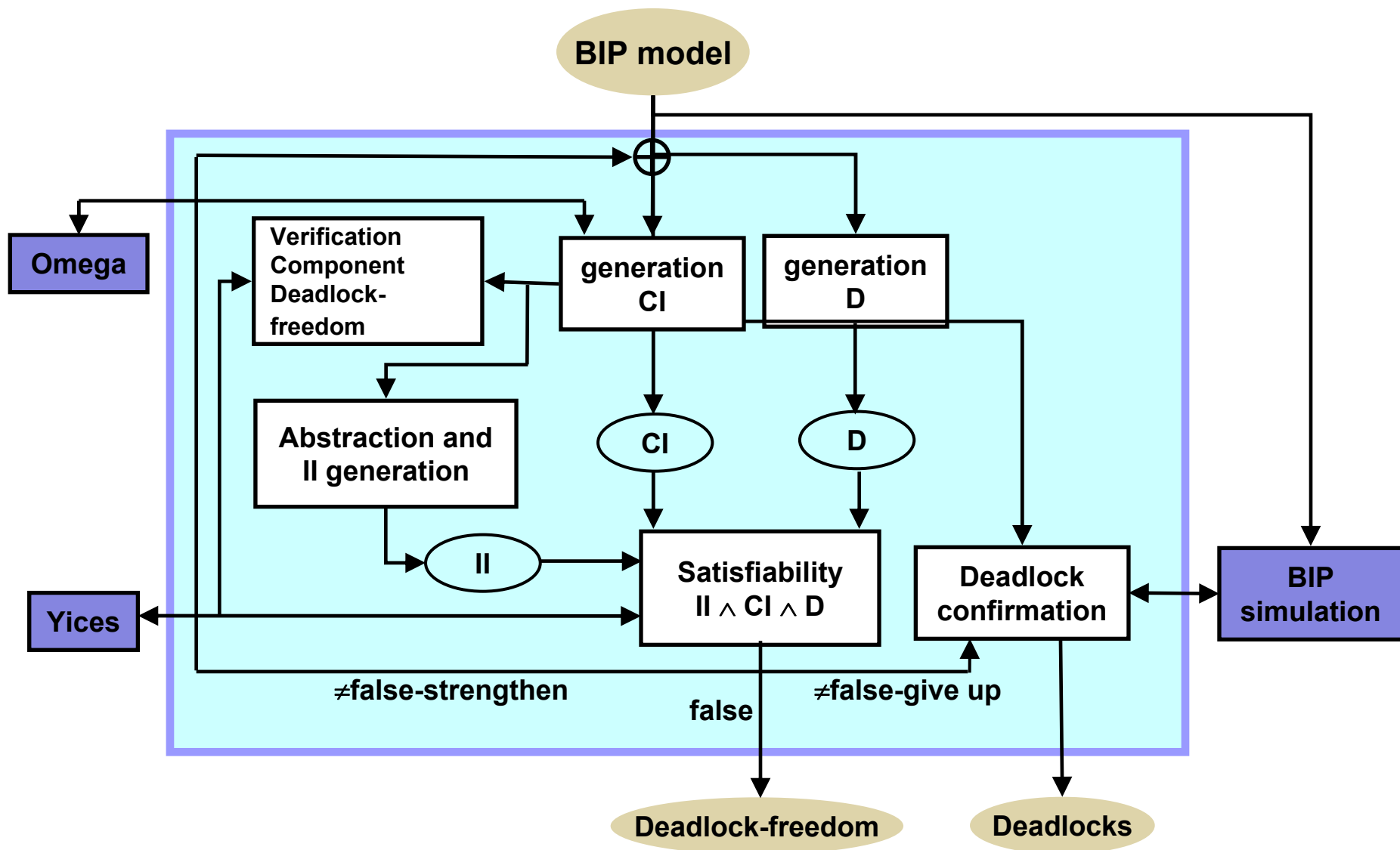
$$\begin{array}{l} z \Rightarrow (y \vee u) \wedge (v \vee r) \\ u \Rightarrow x \vee z \\ v \Rightarrow w \vee z \end{array}$$

$$\begin{array}{l} w \Rightarrow (v \vee r) \\ r \Rightarrow w \vee z \end{array}$$

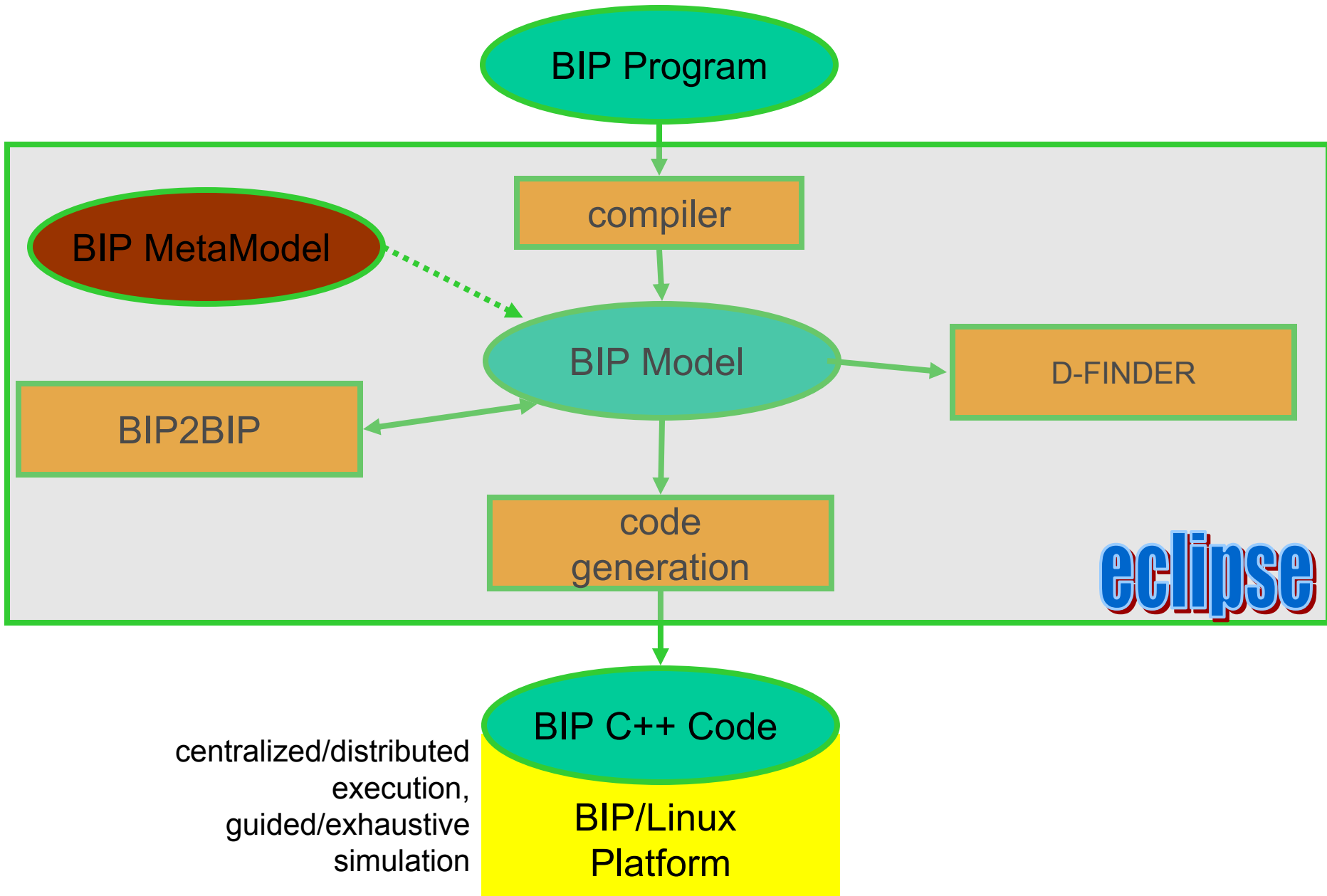
Minimal solutions define invariants :

- Component invariants: $x \vee y$, $z \vee u \vee v$, $w \vee r$
- Interaction invariants: $x \vee u$, $z \vee y \vee v$, $z \vee y \vee r$, $z \vee u \vee r$, $w \vee v$

Compositional Verification – D-Finder



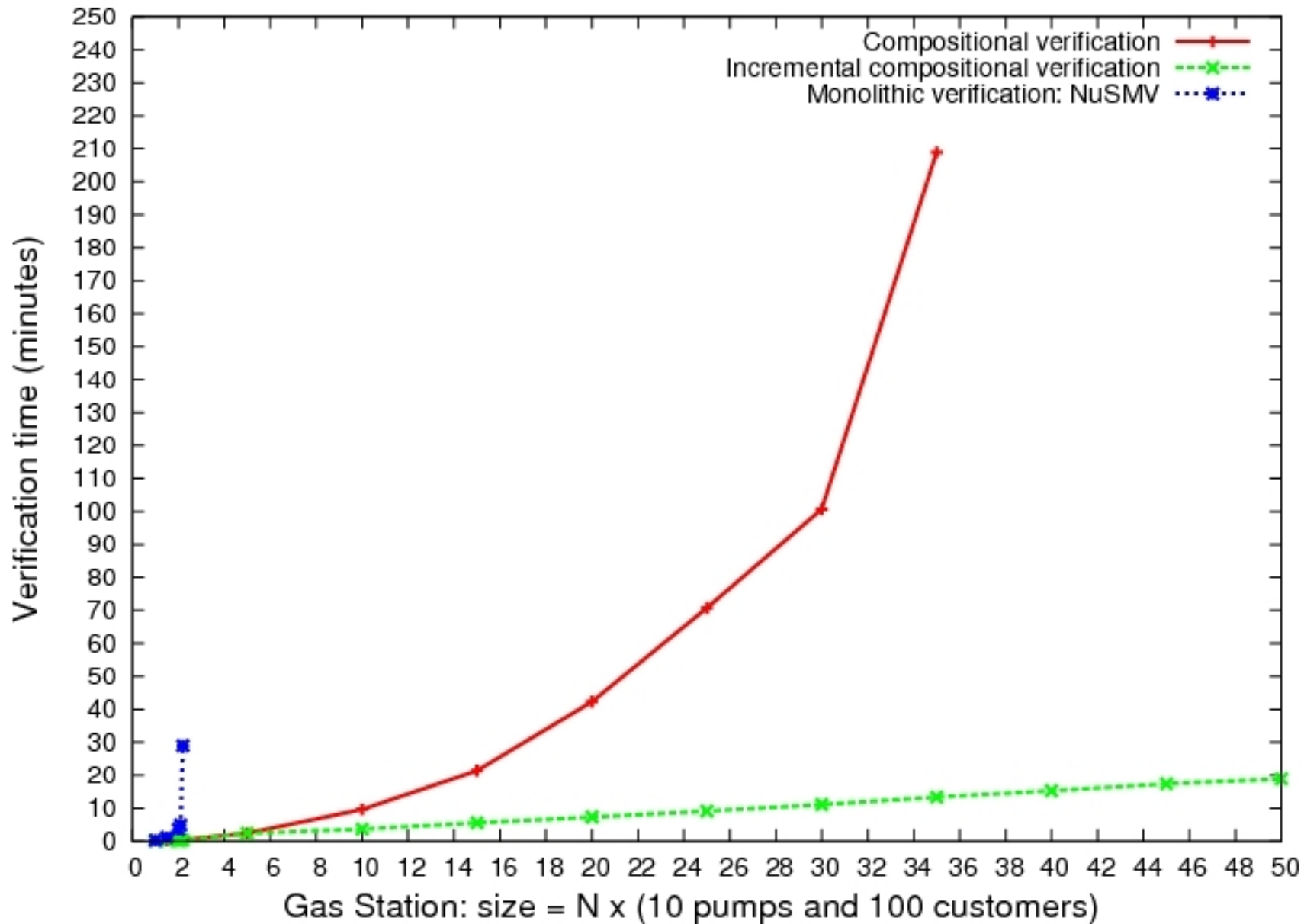
Overall BIP Toolset Architecture

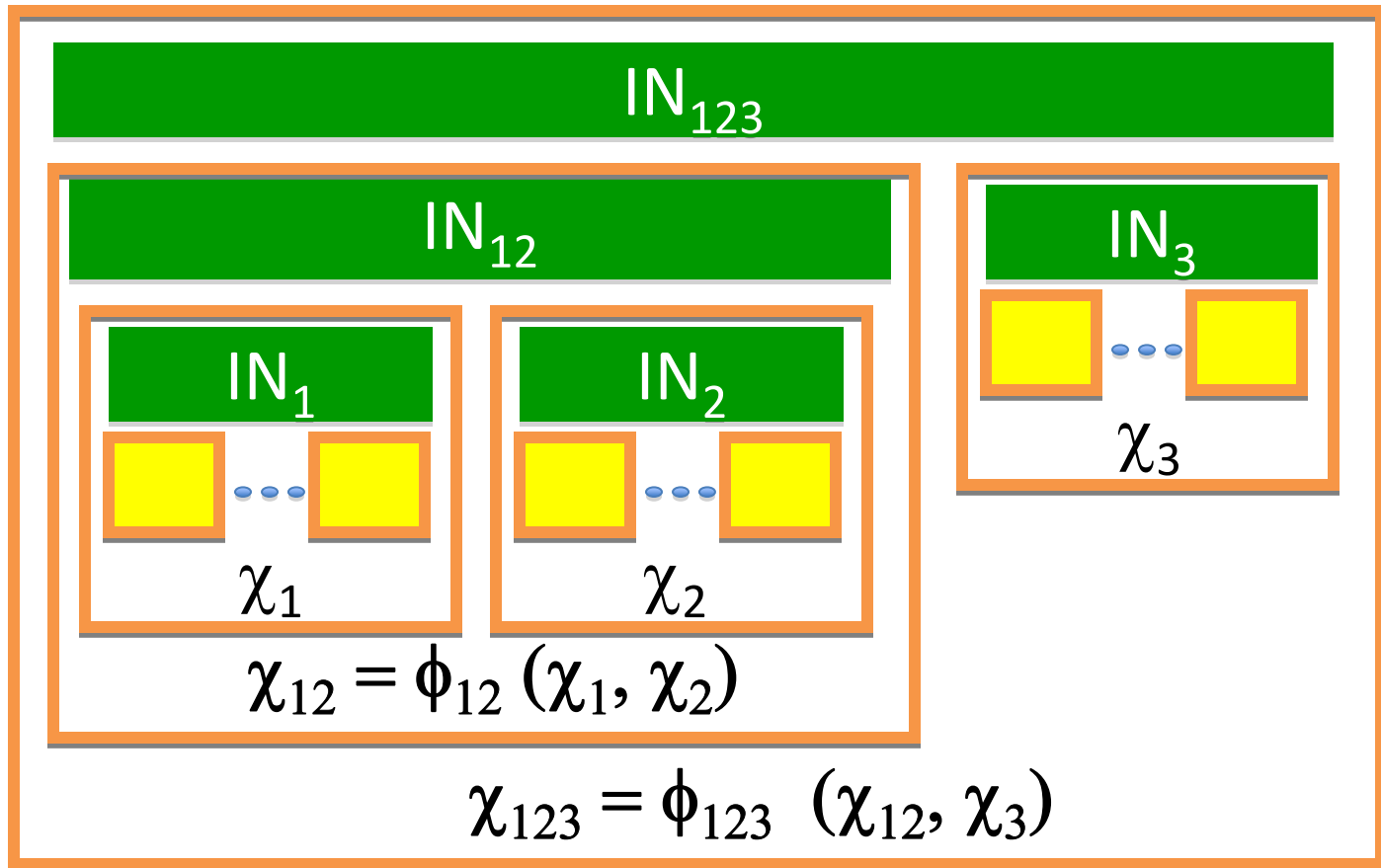


Compositional Verification – D-Finder

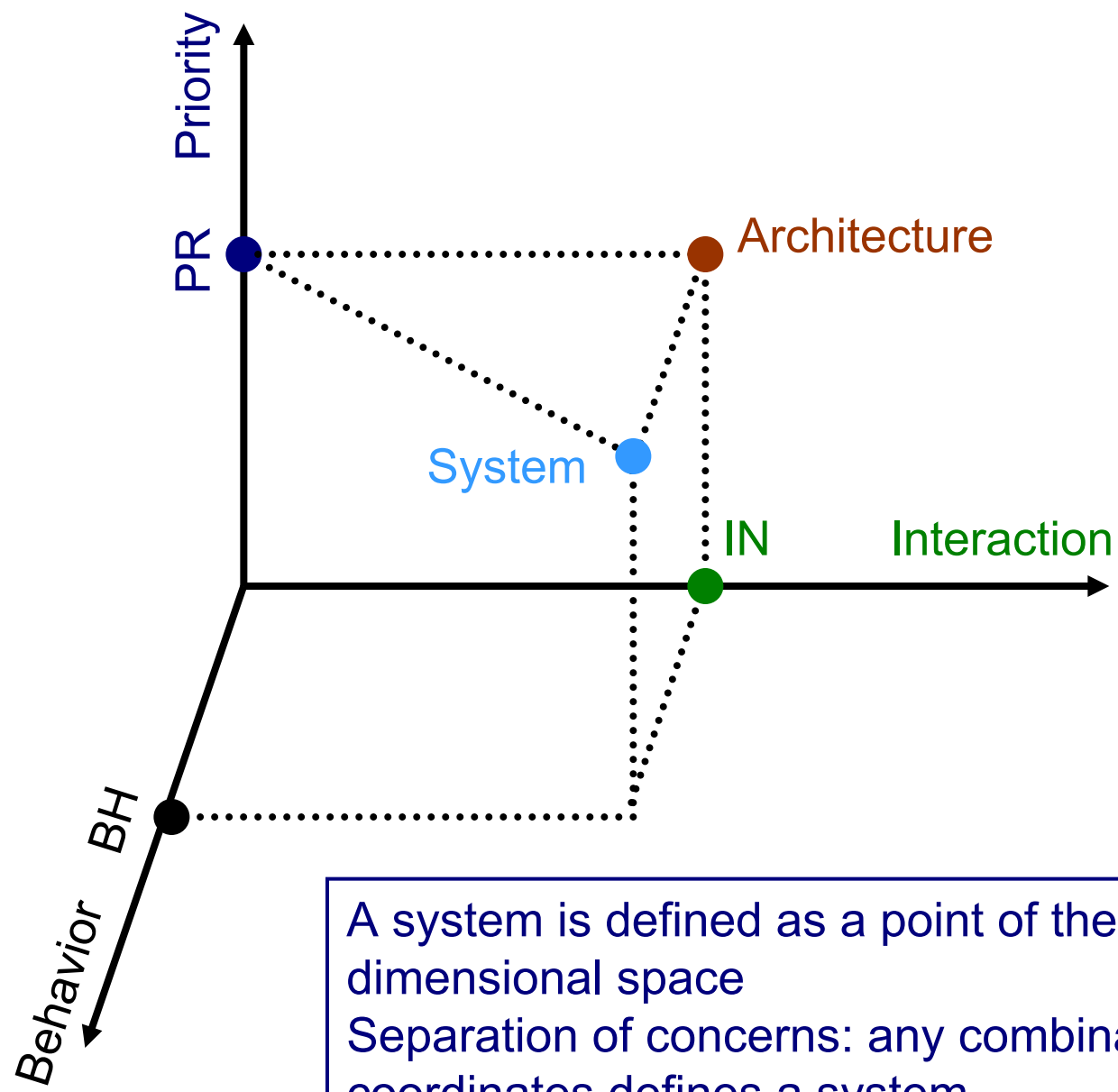
Example	Number of Comp	Number of Ctrl States	Number of Bool Variables	Numb of Int Var	Number Potential Deadlocks	Number Remaining Deadlocks	Verification Time
Temperature Control (2 rods)	3	6	0	3	8	3	3s
Temperature Control (4 rods)	5	10	0	5	32	15	6s
UTOPAR (40 cars,256 CU)	297	795	40	242	--	0	3m46s
UTOPAR (60 cars, 625 CU)	686	1673	60	362	--	0	25m29s
R/W(10000 readers)	10002	20006	0	1	--	0	36m10s
Philosophers (13000)	26000	65000	0	0	--	3	38m48s
Philosophers (10000)	20000	50000	0	0	--	3	29m30s
Smokers (5000)	5001	10007	0	0	--	0	14m
Gas stations (500 pumps, 5000 customers)	5501	21502	0	0	--	0	18m55s

Compositional Verification – D-Finder



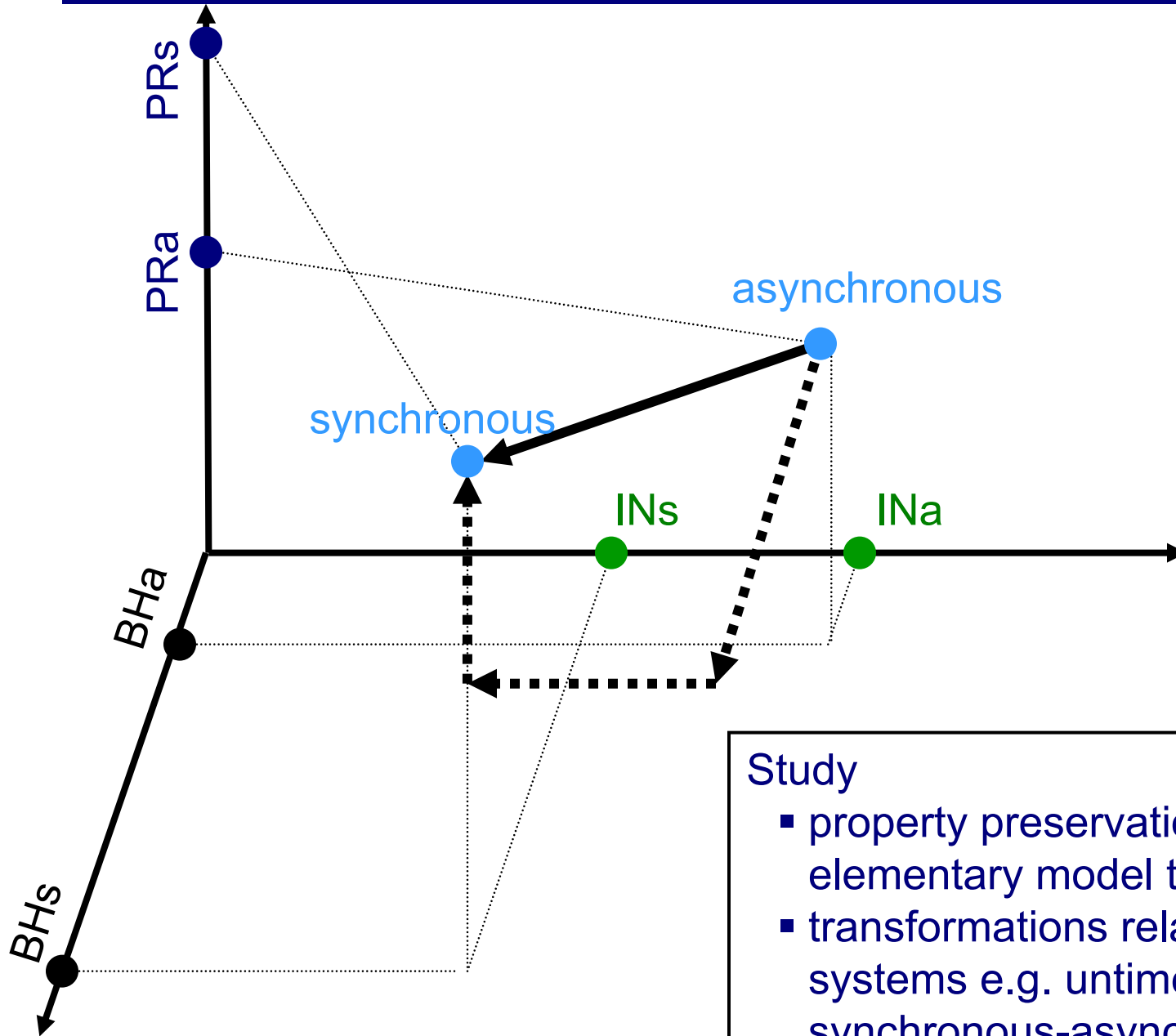


System Construction Space



A system is defined as a point of the 3-dimensional space
Separation of concerns: any combination of coordinates defines a system

System Construction Space – Incrementality

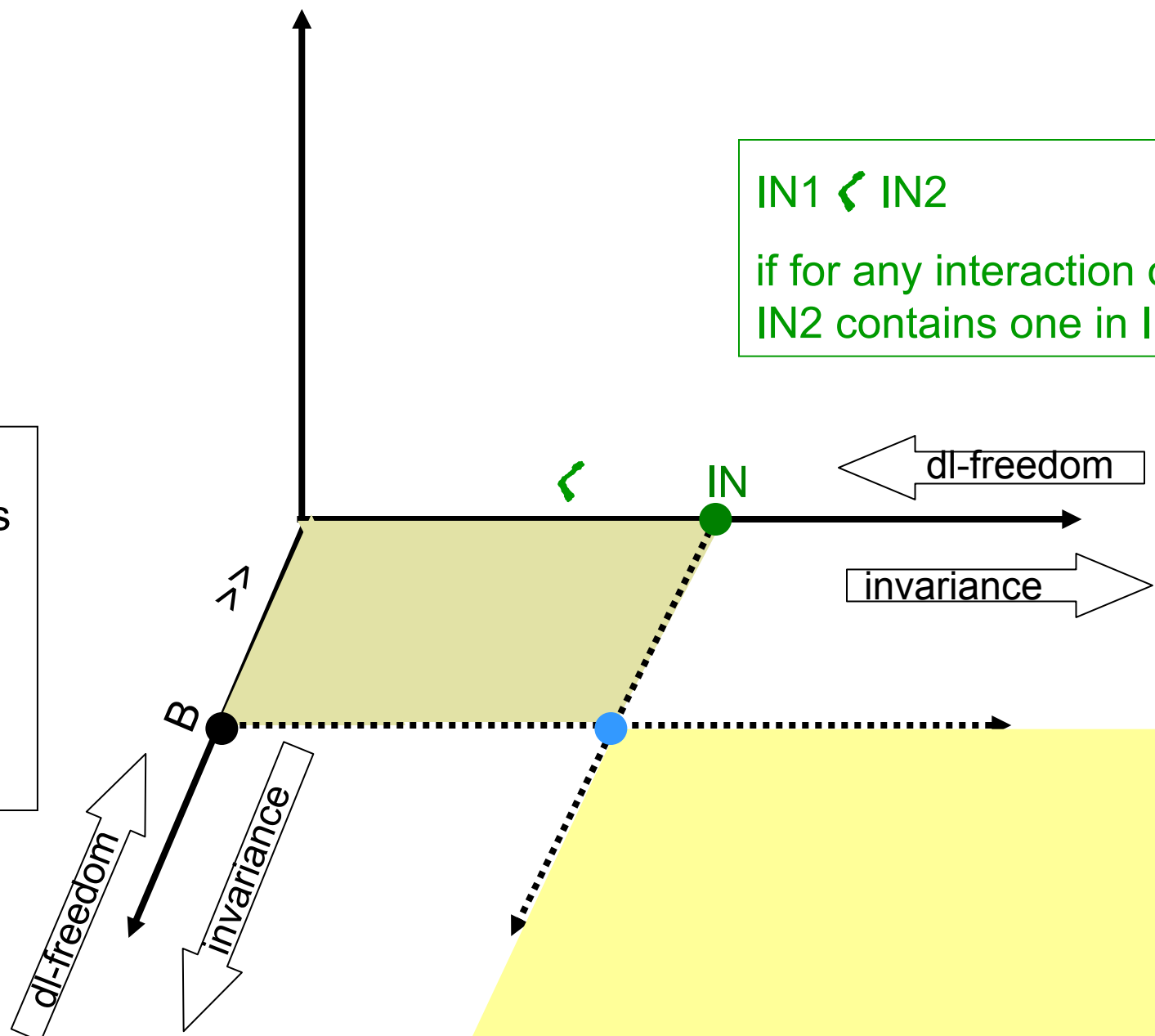


Study

- property preservation results by elementary model transformations
- transformations relating classes of systems e.g. untimed-timed, synchronous-asynchronous

System Construction Space – Incrementality

$B1 \ll B2$ if
B1 simulates
B2 and the
simulation
relation is
total



$IN1 \prec IN2$
if for any interaction of
 $IN2$ contains one in $IN1$



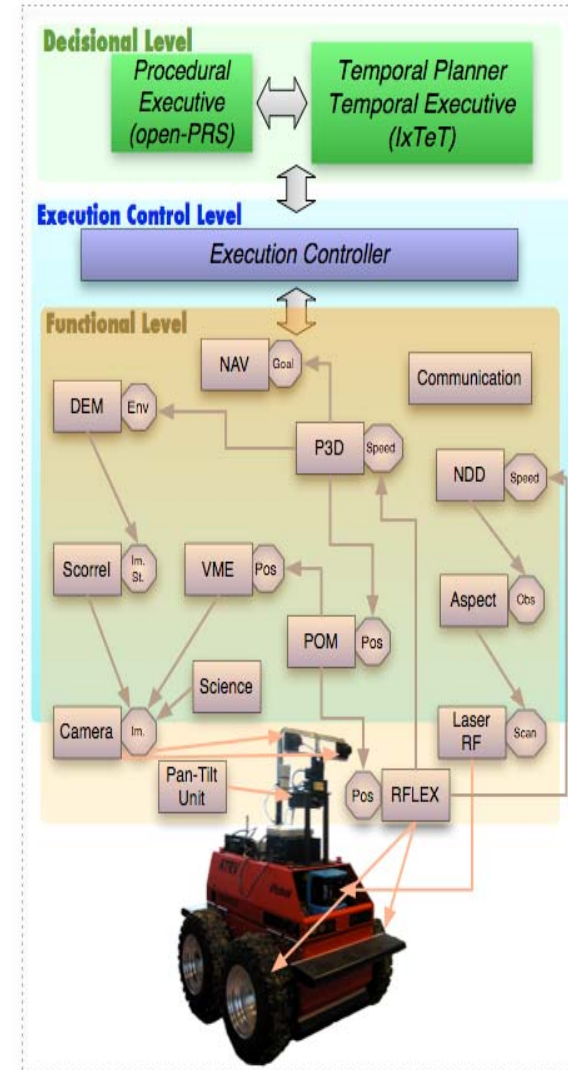
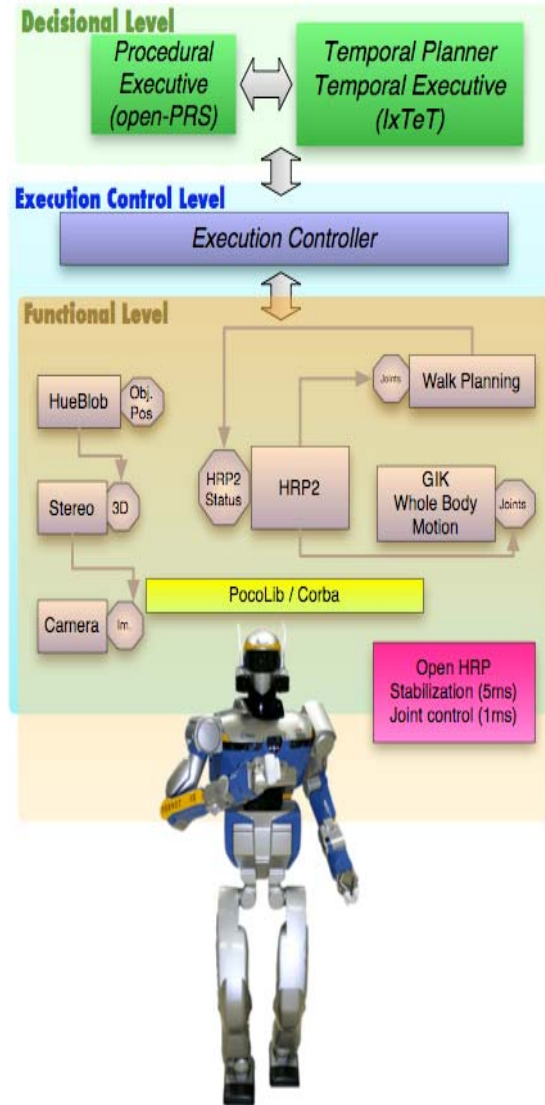
- Current status

- Beyond a posteriori verification

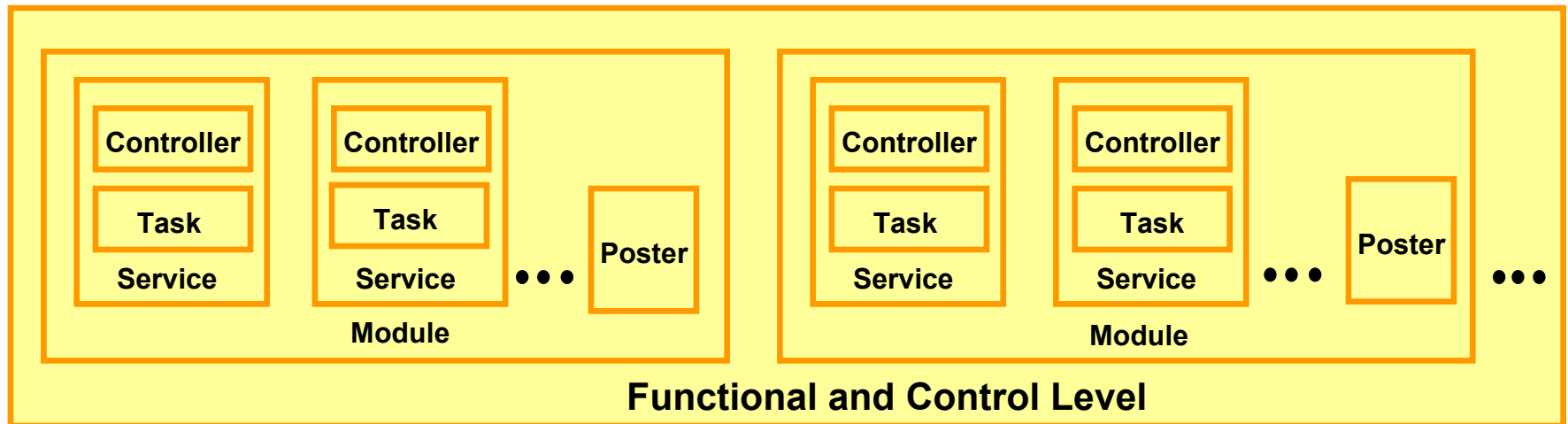
- Component-based Construction
- The BIP Component Framework
- Verification at Design Time

- Conclusion

Autonomous Systems



The DALA Robot – Componentization



Functional and Control Level ::= Module⁺

Module ::= Service⁺ . Poster

Service ::= Service Controller . Service Task

Service Controller ::= Event Triggered Controller | Cyclic Controller

Cyclic Controller ::= Event Triggered Controller . Cyclic Trigger

Service Task ::= Timed Task | Untimed Task

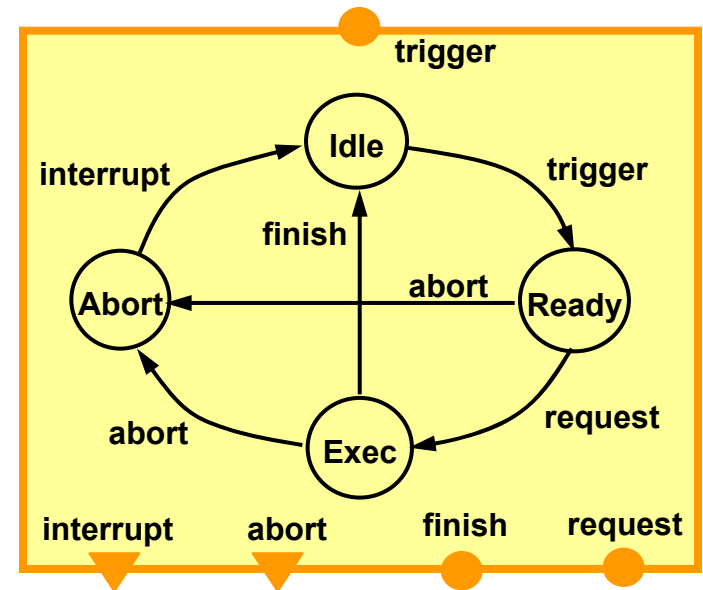
The DALA Robot – Event Triggered Controller

Idle: the Service is idle

Ready: checks the possibility for starting a new Task of the Service

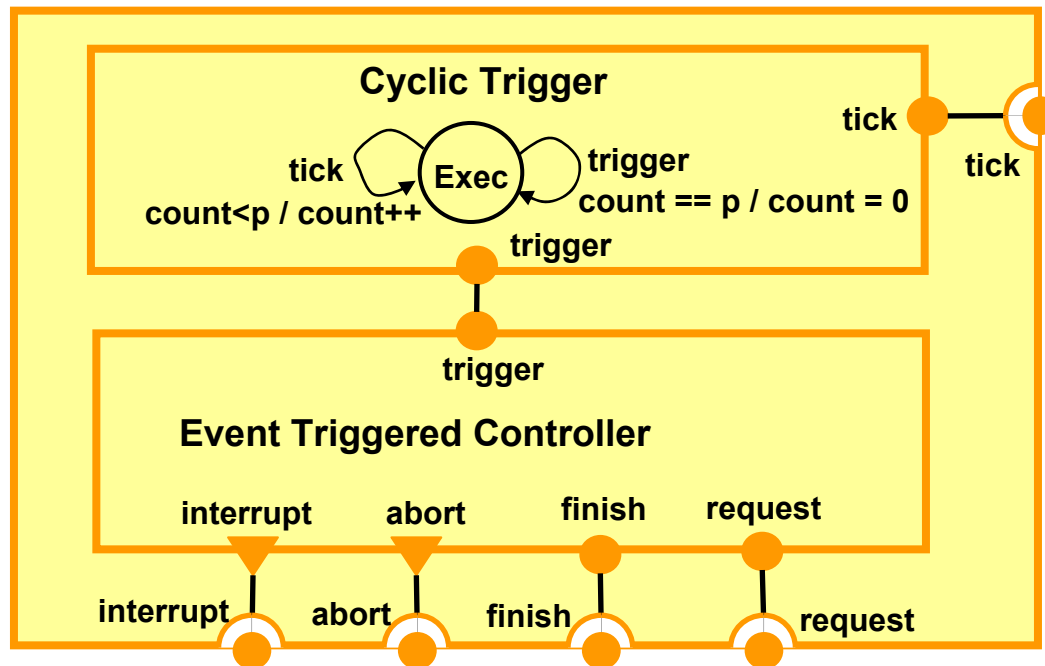
Exec: execution of the Task of the Service

Abort: Service is aborted



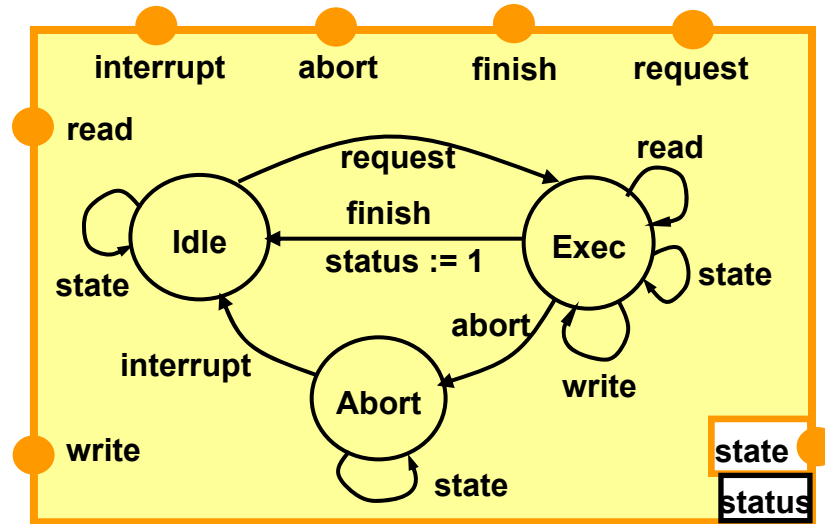
Cyclic Controller ::= Event Triggered Controller . Cyclic Trigger

The Cyclic Trigger starts the Event Triggered Controller every period p



The DALA Robot – Untimed Task

Triggered by *request*

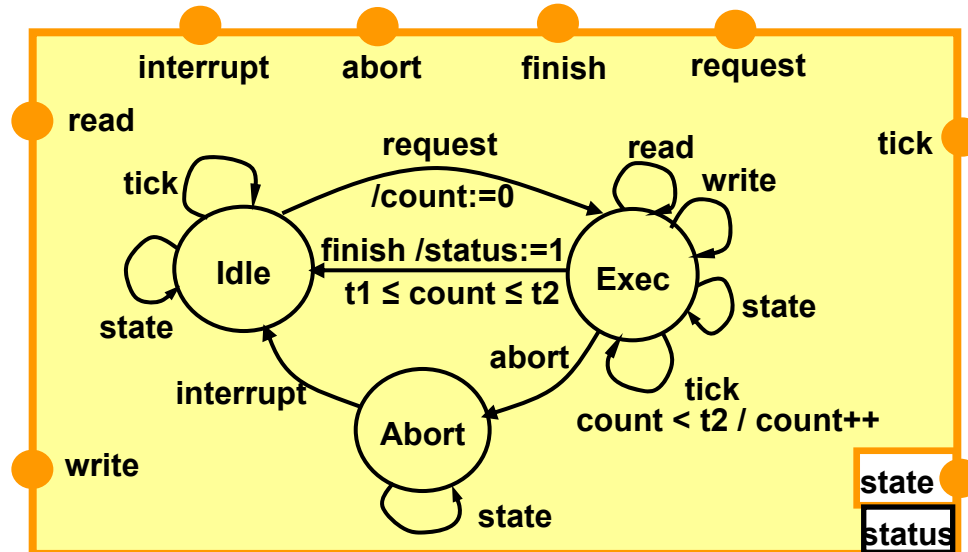


The variable ***status*** specifies the previous state of Task

- status* == 1** : Task successfully executed
- status* == 0** : Task aborted

The DALA Robot – Timed Task

- Obtained from an Untimed Task
- Its execution time is in $[t1, t2]$



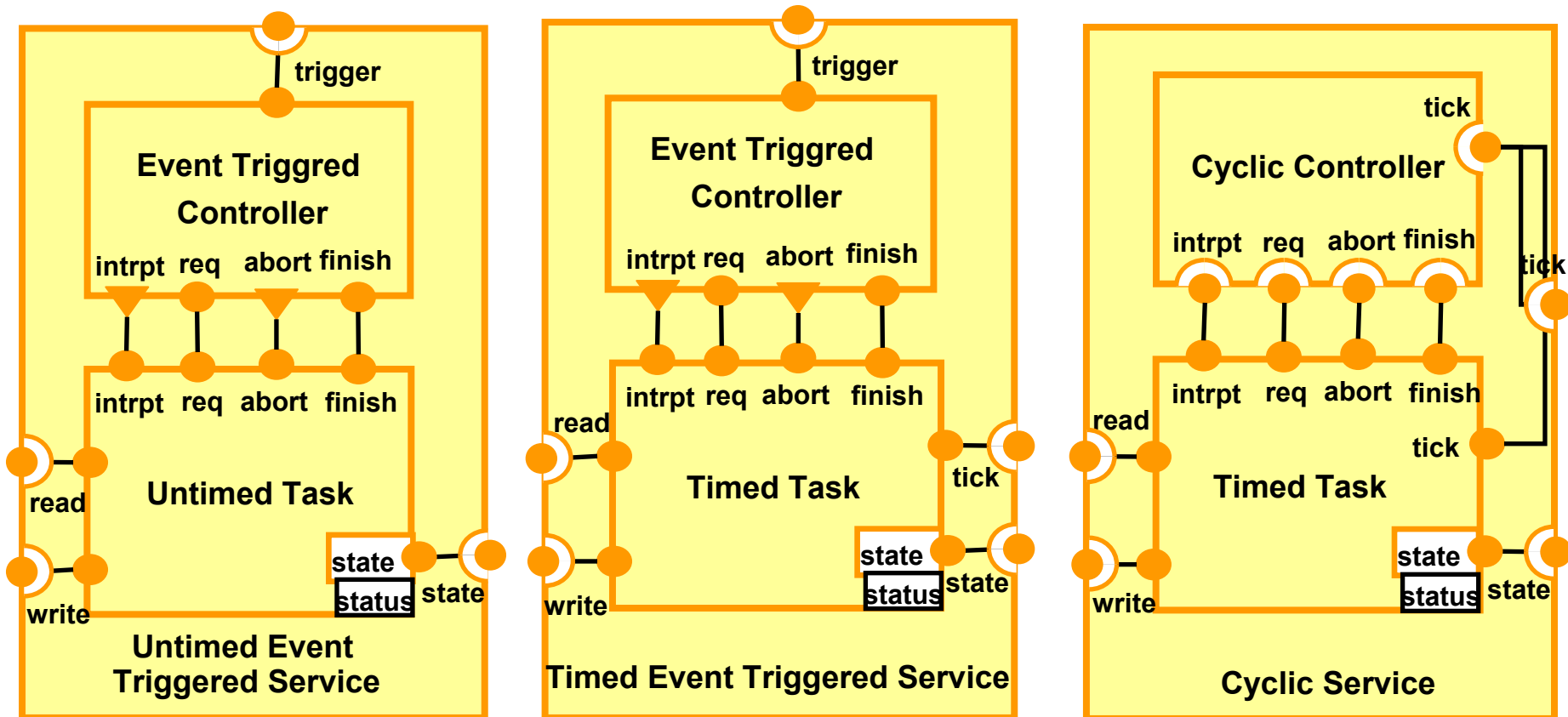
The DALA Robot – Different types of Services

Untimed Event Triggered Service

::= Event Triggered Controller. Untimed Task

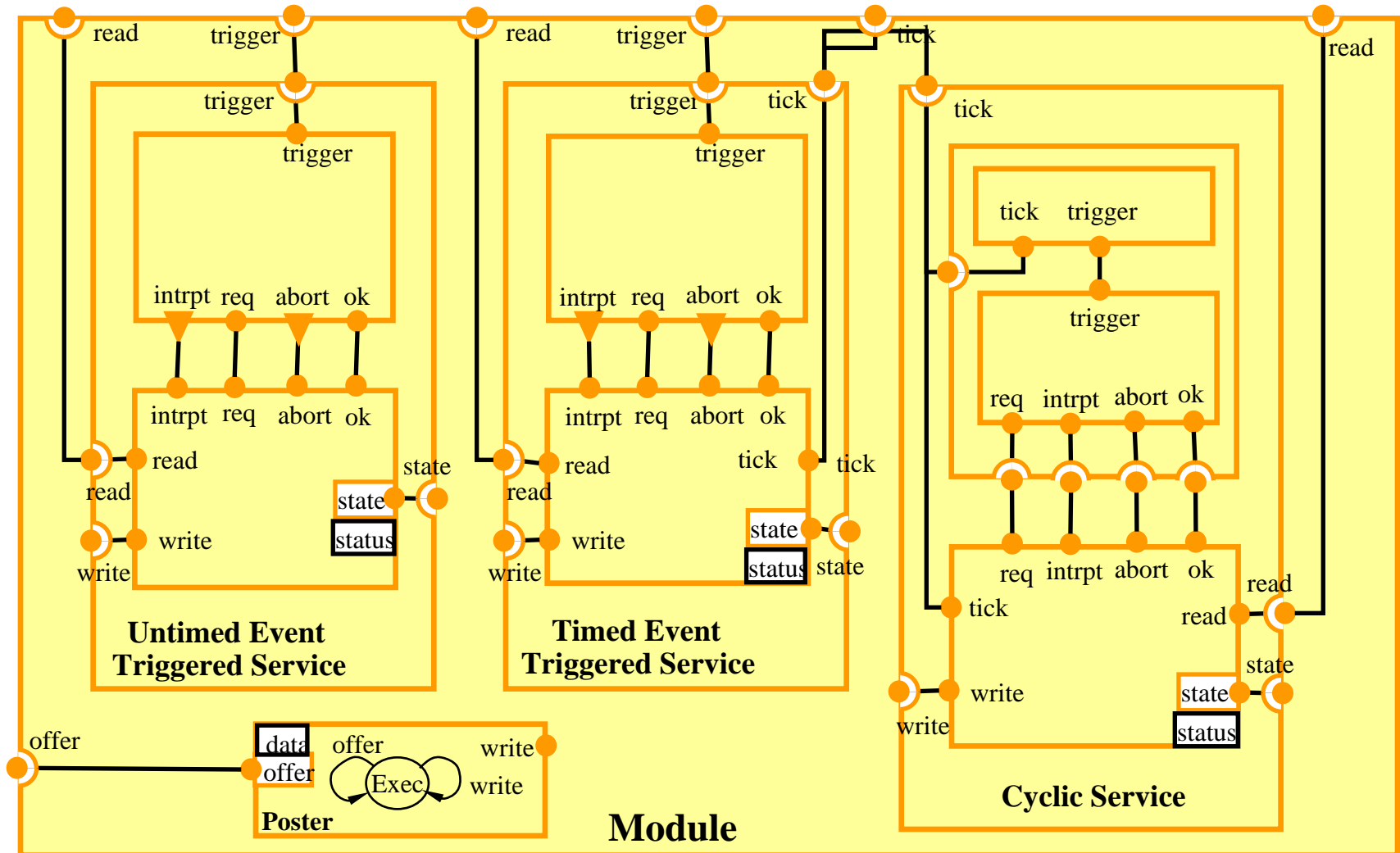
Timed Event Triggered Service ::= Event Triggered Controller. Timed Task

Cyclic Service ::= Cyclic Controller . Timed Task



The DALA Robot – A Module

A module composed of 3 services and a poster



□ Current status

□ Beyond a posteriori verification

- Component-based Construction
- The BIP Component Framework
- Verification at Design Time

□ Conclusion

- ❑ Move from a posteriori verification to verification at design time – adequate framework for component-based construction

- ❑ Minimalistic approach for verification – focus on state invariance and deadlock-freedom

- ❑ Achieve correctness through
 - Constructivity: compositionality/composability techniques
 - Incrementality: reusing proofs for constituents
 - Property-preserving transformations



THANK YOU